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## All-sky Search for Periodic Gravitational Waves in the O1 LIGO Data

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#### Abstract

We report on an all-sky search for periodic gravitational waves in the frequency band $20-475 \mathrm{~Hz}$ and with a frequency time derivative in the range of $[-1.0,+0.1] \times 10^{-8} \mathrm{~Hz} / \mathrm{s}$. Such a signal could be produced by a nearby spinning and slightly non-axisymmetric isolated neutron star in our galaxy. This search uses the data from Advanced LIGO's first observational run, O1. No periodic gravitational wave signals were observed, and upper limits were placed on their strengths. The lowest upper limits on worst-case (linearly polarized) strain amplitude $h_{0}$ are $\sim 4 \times 10^{-25}$ near 170 Hz . For a circularly polarized source (most favorable orientation), the smallest upper limits obtained are $\sim 1.5 \times 10^{-25}$. These upper limits refer to all sky locations and the entire range of frequency derivative values. For a population-averaged ensemble of sky locations and stellar orientations, the lowest upper limits obtained for the strain amplitude are $\sim 2.5 \times 10^{-25}$.


## I. INTRODUCTION

We report the results of an all-sky, multi-pipeline search for continuous, nearly monochromatic gravitational waves from rapidly rotating isolated neutron stars using data from the first observing run (O1) of the Advanced Laser Interferometer Gravitational wave Observatory (Advanced LIGO [1]). Several different analysis algorithms are employed and cover frequencies from 20 Hz through 475 Hz and frequency derivatives over the range $[-1.0,+0.1] \times 10^{-8} \mathrm{~Hz} / \mathrm{s}$.

A number of previous searches for periodic gravitational waves from isolated neutron stars have been carried out in initial LIGO and Virgo data [2 23]. These searches have included coherent searches for gravitational radiation from known radio and X-ray pulsars, directed searches for known stars or locations having unknown signal frequencies, and spotlight or all-sky searches for stars with unknown signal frequency and sky location.

Here, we apply four different all-sky search programs (pipelines) used in previous searches. In summary,

- The PowerFlux pipeline has been used in previous searches of initial LIGO data from the S4, S5 and S6 Science Runs [12, 14, 16, 20. The program uses a Loosely Coherent method for following up outliers [24], and also a new universal statistic that provides correct upper limits regardless of the noise distribution of the underlying data, but which yields near-optimal performance for Gaussian data [25].
- The FrequencyHough hierarchical pipeline has been used in the previous all-sky search of Virgo VSR2 and VSR4 Science Runs [23]. It consists of an initial multi-stage phase, in which candidates are pro-
duced, and a follow-up phase in which the candidates are confirmed or discarded. Frequentist upper limits are computed with a computationally cheap procedure, based on the injection of a large number of simulated signals into the data.
- The SkyHough pipeline has been used in previous searches of initial LIGO data from the S2, S4 and S5 Science Runs [11, 12, 18, as well as in the second stage of Einstein@Home searches [13, 15]. An improved pipeline, applying a clustering algorithm to coincident candidates was employed in 26]. Frequentist upper limits are derived based on a number of simulated software signal injections into the data.
- The Time-Domain $\mathcal{F}$-statistic pipeline has been used in the all-sky search of the Virgo VSR1 data [19. This program performs a coherent analysis of narrow-band time-domain sequences (each a few days long) with the $\mathcal{F}$-statistic method [27, followed by a search for coincidences among candidates found in different time sequences, for a given band. In order to estimate the sensitivity, frequentist upper limits are obtained by injecting simulated signals into the data.

These different analysis programs employ a variety of algorithmic and parameter choices, in order to reduce the possibility of discarding a gravitational wave signal due to sub-optimal treatment of detector artifacts or by adhering to an overly restrictive signal model. The coherence times used in first-stage data processing range from 1800 s to 6 days, and the treatment of narrow spectral artifacts ("lines") differs substantially among the different search programs. The latter is an especially important
consideration for the O1 data set, because lines are, unfortunately, especially prevalent.

After following up the first-stage outliers, none of the different search pipelines found evidence for continuous gravitational waves in the O1 data over the range of frequencies and frequency derivatives searched. Upper limits are derived for each analysis, with some variation in techniques among the different programs.

This article is organized as follows: Sec.IIdescribes the Advanced LIGO interferometers and the first observing run. Sec. III provides an overview of the four pipelines, discussing common and differing features. The individual pipelines are described in more detail in sec. IV. In sec $V$. the results of these four searches are presented; describing both the outliers and their follow up, and the derived upper limits. Finally, we conclude in sec. VI.

## II. LIGO INTERFEROMETERS AND THE O1 OBSERVING RUN

Advanced LIGO consists of two detectors, one in Hanford, Washington, and the other in Livingston, Louisiana, separated by a $\sim 3000-\mathrm{km}$ baseline [28]. Each site hosts one, 4 -km-long interferometer inside a vacuum envelope with the primary interferometer optics suspended by a cascaded, quadruple suspension system in order to isolate them from external disturbances. The interferometer mirrors act as test masses, and the passage of a gravitational wave induces a differential-arm length change which is proportional to the gravitational-wave strain amplitude. The Advanced LIGO detectors began data collecting in September 2015 after a major upgrade targeting a 10 -fold improvement in sensitivity over the initial LIGO detectors. While not yet operating at design sensitivity, both detectors reached an instrument noise 3 to 4 times lower than the previous best with the initialgeneration detectors in their most sensitive frequency band between 100 Hz and 300 Hz [29].

Advanced LIGO's first observing run occurred between September 12, 2015 and January 19, 2016, for which approximately 77 days and 66 days of analyzable data was produced by the Hanford (H1) and Livingston (L1) interferometers, respectively. Notable instrumental contaminations affecting the searches described here included spectral combs of narrow lines in both interferometers, many of which were identified after the run ended and mitigated for future running. These artifacts included an $8-\mathrm{Hz}$ comb in H 1 with the even harmonics $(16-\mathrm{Hz}$ comb) being especially strong, which was later tracked down to digitization roundoff error in a high-frequency excitation applied to servo-control the cavity length of the Output Mode Cleaner (OMC). Similarly, a set of lines found to be linear combinations of 22.7 Hz and 25.6 Hz in the L1 data was tracked down to OMC excitation at a still higher frequency, for which digitization error occurred.

In addition, the low-frequency band of the H 1 and L1 data (below $\sim 140 \mathrm{~Hz}$ ) was heavily contaminated by
combs with spacings of 1 Hz , near- $1-\mathrm{Hz}$ and $0.5-\mathrm{Hz}$ and a variety of non-zero offsets from harmonicity. Many of these lines originated from the observatory timing system, which includes both GPS-locked clocks and freerunning local oscillators. The couplings into the interferometer appeared to come primarily through common current draws among power supplies in electronics racks. These couplings were reduced following O1 via isolation of power supplies, and in some cases, reduction of periodic current draws in the timing system itself (blinking LEDs). A subset of these lines with common origins at the two observatories contaminated the O1 search for a stochastic background of gravitational waves, which relies upon cross-correlation of H1 and L1 data, requiring excision of affected bands 30.

Although most of these strong and narrow lines are stationary in frequency and hence do not exhibit the Doppler modulations due to the Earth's motion expected for a continuous wave (CW) signal from most sky locations, the lines pollute the spectrum for such sources. In sky locations near the ecliptic poles, the lines contribute extreme contamination for certain signal frequencies. For a run like O1 that spans only a modest fraction of a full year, there are also other regions of the sky and spindown parameter space for which the Earth's average acceleration toward the Sun largely cancels a non-zero source frequency derivative, leading to signal templates with substantial contamination from stationary instrumental lines [12]. The search programs used here have chosen a variety of methods to cope with this contamination, as described below.

## III. OVERVIEW OF SEARCH PIPELINES

The four search pipelines have many features in common, but also have important differences, both major and minor. In this section we provide a broad overview of similarities and differences before describing the individual pipelines in more detail in the following section.

## A. Signal Model

All four search methods presented here assume the same signal model, based on a classical model of a spinning neutron star with a time-varying quadrupole moment that produces circularly polarized gravitational radiation along the rotation axis and linearly polarized radiation in the directions perpendicular to the rotation axis. The linear polarization is the most unfavorable case because the gravitational wave flux impinging on the detectors is smallest compared to the flux from circularly polarized waves.

The assumed strain signal model for a periodic source
is given as

$$
\begin{align*}
h(t)= & h_{0}\left(F_{+}\left(t, \alpha_{0}, \delta_{0}, \psi\right) \frac{1+\cos ^{2}(\iota)}{2} \cos (\Phi(t))+\right.  \tag{1}\\
& \left.+F_{\times}\left(t, \alpha_{0}, \delta_{0}, \psi\right) \cos (\iota) \sin (\Phi(t))\right)
\end{align*}
$$

where $F_{+}$and $F_{\times}$characterize the detector responses to signals with " + " and " $\times$ " quadrupolar polarizations [12, [14, 16, the sky location is described by right ascension $\alpha_{0}$ and declination $\delta_{0}, \psi$ is the polarization angle of the projected source rotation axis in the sky plane, and the inclination of the source rotation axis to the detector line-of-sight is $\iota$. The phase evolution of the signal is given by the formula

$$
\begin{equation*}
\Phi(t)=2 \pi\left(f_{\text {source }} \cdot\left(t-t_{0}\right)+f^{(1)} \cdot\left(t-t_{0}\right)^{2} / 2\right)+\phi \tag{2}
\end{equation*}
$$

where $f_{\text {source }}$ is the source frequency, $f^{(1)}$ is the first frequency derivative (which, when negative, is termed the spindown), time in the Solar System barycenter is $t$, and the initial phase $\phi$ is computed relative to reference time $t_{0}$. When expressed as a function of local time of groundbased detectors, Eq. 2 acquires sky-position-dependent Doppler shift terms.

Most natural sources are expected to have a negative first frequency derivative, as the energy lost in gravitational or electromagnetic waves would make the source spin more slowly. The frequency derivative can be positive when the source is affected by a strong slowly-varying Doppler shift, such as due to a long-period orbit with a companion.

## B. Detection Statistics

All four methods look for excess detected strain power that follows a time evolution of peak frequency consistent with the signal model. Each program begins with sets of "short Fourier transforms" (SFTs) that span the observation period, with coherence times ranging from 1800 to 7200 s. The first three pipelines (PowerFlux, FrequencyHough and SkyHough) compute measures of strain power directly from the SFTs and create detection statistics by stacking those powers or stacking weights for powers exceeding threshold, with corrections for frequency evolution applied in the semi-coherent power stacking. The fourth pipeline (Time-Domain $\mathcal{F}$-statistic) uses a much longer coherence time ( 6 d ) and applies frequency evolution corrections coherently in band-limited timedomain data recreated from the SFT sets, to obtain the $\mathcal{F}$-statistic [27]. Coincidences are then required among multiple data segments with no stacking.

The PowerFlux method includes explicit searches over different signal polarizations, while the other three methods use a detection statistic that performs well on average over an ensemble of polarizations.

All methods search for initial frequency in the range $20-2000 \mathrm{~Hz}$, but with template grid spacings that depend inversely upon the effective coherence time used.

The range of $\dot{f}$ values searched is $\left[-1 \times 10^{-8},+1 \times\right.$ $\left.10^{-9}\right] \mathrm{Hz} \mathrm{s}^{-1}$. All known isolated pulsars spin down more slowly than the two values of $|\dot{f}|_{\text {max }}$ used here, and as seen in the results section, the ellipticity required for higher $|\dot{f}|$ is improbably high for a source losing rotational energy primarily via gravitational radiation at low frequencies. A small number of isolated pulsars in globular clusters exhibit slight spin-up, believed to arise from acceleration in the Earth's direction; such spin-up values have magnitudes small enough to be detectable with the zero-spin-down templates used in these searches, given a strong enough signal. Another potential source of apparent spin-up is Dopper modulation from an unseen, long-period binary companion.

## C. Upper limits

While the parameter space searched is the same for the three methods, there are important differences in the way upper limits are determined. The PowerFlux pipeline sets strict frequentist upper limits on detected strain power in circular and linear polarizations that apply everywhere on the sky except for small regions near the ecliptic poles, where signals with small Doppler modulations can be masked by stationary instrumental spectral lines. The other three pipelines set population-averaged upper limits over the parameter search volume, relying upon Monte Carlo simulations.

## D. Outlier follow-up

The PowerFlux and FrequencyHough pipelines have hierarchical structures that permit systematic follow-up of loud outliers in the initial stage to improve intrinsic strain sensitivity by increasing effective coherence time while dramatically reducing the parameter space volume over which the follow-up is pursued. The PowerFlux pipeline uses "loose coherence" [24] with stages of improving refinement via steadily increasing effective coherence times, while the FrequencyHough pipeline increases the effective coherence time by a factor of 10 and recomputes strain power "peakmaps." Any outliers that survive all stages of any of the four pipelines are examined manually for contamination from known instrumental artifacts and for evidence of contamination from a previously unknown single-interferometer artifact. Those for which no artifacts are found are subjected to additional systematic follow-up used for Einstein@Home searches [31, 32], which includes a final stage with full coherence across the entire data run.

## IV. DETAILS OF SEARCH METHODS

## A. PowerFlux Search Method

The PowerFlux search pipeline has two principal stages. First, the main PowerFlux algorithm [12, 14, 16, $33-35$ is run to establish upper limits and produce lists of outliers with signal-to-noise ratio (SNR) greater than a threshold of 5 . These outliers are then followed up with the Loosely Coherent detection pipeline [16, 24, 36, which is used to reject or confirm the outliers.

Both algorithms calculate power for a bank of signal model templates. The upper limits and signal-to-noise ratios for each template are computed by comparison to templates with nearby frequencies and the same sky location and spindown [25, 33, 34]. The calibrated detector output time series, $h(t)$, for each detector, is broken into $50 \%$-overlapping 7200 s-long segments which are Hannwindowed and Fourier-transformed. The resulting Short Fourier Transforms (SFTs) are arranged into an input matrix with time and frequency dimensions. The power calculation of the data can be expressed as a bilinear form of the input matrix $\left\{a_{t, f}\right\}$ :

$$
\begin{equation*}
P[f]=\sum_{t_{1}, t_{2}} a_{t_{1}, f+\Delta f\left(t_{1}\right)} a_{t_{2}, f+\Delta f\left(t_{2}\right)}^{*} K_{t_{1}, t_{2}, f} \tag{3}
\end{equation*}
$$

where $\Delta f(t)$ is the detector frame frequency drift due to the effects from both Doppler shifts and the first frequency derivative. The sum is taken over all times $t$ corresponding to the midpoint of the short Fourier transform time interval. The kernel $K_{t_{1}, t_{2}, f}$ includes the contribution of time dependent SFT noise weights, antenna response, signal polarization parameters, and relative phase terms [24, 36].

The first-stage, PowerFlux algorithm uses a kernel with main diagonal terms only and is very fast. The second-stage, Loosely Coherent algorithm increases coherence time while still allowing for controlled deviation in phase [24]. This is done by more complicated kernels that increase effective coherence length.

The effective coherence length is captured in a parameter $\delta$, which describes the amount of phase drift that the kernel allows between SFTs. A value of $\delta=0$ corresponds to a fully coherent case, and $\delta=2 \pi$ corresponds to incoherent power sums.

Depending on the terms used, the data from different interferometers can be combined incoherently (such as in stages 0 and 1, see Table (I) or coherently (as used in stages 2,3 and 4). The coherent combination is more computationally expensive but provides much better parameter estimation.

The upper limits presented in section V B (Figure 15) are reported in terms of the worst-case value of $h_{0}$ (which applies to linear polarizations with $\iota=\pi / 2$ ) and for the most sensitive circular polarization $(\iota=0$ or $\pi)$. As described previously [16, the pipeline retains some sen-
sitivity, however, to non-general-relativity GW polarization models, including a longitudinal component, and to slow amplitude evolution.

The $95 \%$ confidence level upper limits (see Figure 15) produced in the first stage are based on the overall noise level and largest outlier in strain found for every template in each 62.5 mHz band in the first stage of the pipeline. The 62.5 mHz bands are analyzed by separate instances of PowerFlux [16]. A followup search for detection is carried out for high-SNR outliers found in the first stage.

## 1. Universal statistics

As discussed above, a multitude of spectral combs contaminated the O1 low-frequency band, and, in contrast to the 23 -month-long S5 Science Run and 15-month-long S6 Science Runs of initial LIGO, the 4-month-long O1 run did not span the Earth's full orbit. This means the Doppler shift magnitudes from the Earth's motion are reduced, on the whole, in O1 compared to those of the other, earlier runs. In particular, for certain combinations of sky location, frequency and spindown, a signal can appear relatively stationary in frequency in the detector frame of reference. This effect is most pronounced for low signal frequencies, a pathology noted in searches of the 1 -month-long S 4 run [12]. At the same time, putative signals with low frequencies permit the use of $7200-\mathrm{s}$ SFT spans, longer than the typical 1800-s SFTs used in the past, which helps to resolve stationary instrumental lines from signals. One downside, though, of longer coherence length is that there are far fewer SFTs in power sums compared with previous runs, which contributes to larger deviations from ideal Gaussian behavior for powersum statistics.

To allow robust analysis of the entire spectrum, including the especially challenging lowest frequencies, the Universal statistic algorithm [25] is used for establishing upper limits. The algorithm is derived from the Markov inequality and shares its independence from the underlying noise distribution. It produces upper limits less than $5 \%$ above optimal in case of Gaussian noise. In nonGaussian bands, it can report values larger than what would be obtained if the distribution were known, but the upper limits are always at least $95 \%$ valid. Figure 1 shows results of an injection run performed as described in [16. Correctly established upper limits lie above the red line.

## 2. Outlier follow-up

The initial stage (labeled 0) scans the entire sky with the semi-coherent PowerFlux algorithm that computes weighted sums of powers of 7200 s Hann-windowed SFTs. These power sums are then analyzed to identify highSNR outliers. A separate algorithm uses the universal statistic [25] to establish upper limits.

| Stage | Instrument sum | Phase coherence rad | $\begin{gathered} \text { Spindown step } \\ \mathrm{Hz} / \mathrm{s} \\ \hline \end{gathered}$ | Sky refinement | Frequency refinement | $\begin{gathered} \text { SNR increase } \\ \% \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | Initial/upper limit semi-coherent | NA | $1 \times 10^{-10}$ | 1 | 1/2 | NA |
| 1 | incoherent | $\pi / 2$ | $1.0 \times 10^{-10}$ | 1/4 | 1/8 | 20 |
| 2 | coherent | $\pi / 2$ | $5.0 \times 10^{-11}$ | 1/4 | 1/8 | 10 |
| 3 | coherent | $\pi / 4$ | $2.5 \times 10^{-11}$ | 1/8 | 1/16 | 10 |
| 4 | coherent | $\pi / 8$ | $5.0 \times 10^{-12}$ | 1/16 | 1/32 | 7 |

TABLE I. PowerFlux analysis pipeline parameters. Starting with stage 1, all stages used the Loosely Coherent algorithm for demodulation. The sky and frequency refinement parameters are relative to values used in the semicoherent PowerFlux search.


FIG. 1. PowerFlux upper limit validation. Each point represents a separate injection in the $50-200 \mathrm{~Hz}$ frequency range. Each established upper limit (vertical axis) is compared against the injected strain value (horizontal axis, red line) (color online).

The outlier follow-up procedure used in [16, 20 has been extended with additional stages (see Table I) to reduce the larger number of initial outliers, expected because of non-Gaussian artifacts and larger initial search space.

The entire dataset is partitioned into 3 stretches of equal length, and power sums are produced independently for any contiguous combinations of these stretches. As is done in [20, 22], the outlier identification is performed independently in each stretch.

High-SNR outliers are subject to a coincidence test. For each outlier with $\mathrm{SNR}>7$ in the combined H1 and L1 data, we require there to be outliers in the individual detector data of the same sky area that had $\mathrm{SNR}>5$, matching the parameters of the combined-detector outlier within $83 \mu \mathrm{~Hz}$ in frequency, and $7 \times 10^{-11} \mathrm{~Hz} / \mathrm{s}$ in spindown. The combined-detector SNR is additionally required to be above both single-detector SNRs.

The identified outliers using combined data are then passed to the followup stage using the Loosely Coherent algorithm 24 with progressively tighter phase coherence parameters $\delta$, and improved determination of frequency, spindown, and sky location.

As the initial stage 0 sums only powers, it does not use the relative phase between interferometers, which results in some degeneracy among sky position, frequency, and spindown. The first Loosely Coherent followup stage also combines interferometer powers incoherently, but demands greater temporal coherence (smaller $\delta$ ) within each interferometer, which should boost the SNR of viable outliers by at least $20 \%$. Subsequent stages use data coherently, providing tighter bounds on outlier location.

Testing of the pipeline was performed for frequencies above 50 Hz . Injection recovery efficiencies from simulations covering the $50-200 \mathrm{~Hz}$ range are shown in Figure 2 . The same followup parameters were applied to the $20-50 \mathrm{~Hz}$ region, but with stage 0 utilizing twice as dense spindown stepping.

Because the followup parameters were not tuned for the $20-50 \mathrm{~Hz}$ low frequency region and because of the highly disturbed spectrum, we do not expect a $95 \%$ recovery rate.

Only a mild influence from parameter mismatch is expected, as the parameters are chosen to accommodate the worst few percent of injections. The followup procedure establishes very wide margins for outlier followup. For example, when transitioning from the semi-coherent stage 0 to the Loosely Coherent stage 1, the effective coherence length increases by a factor of 4 . The average true signal SNR should then increase by more than $40 \%$. But the threshold used in followup is only $20 \%$, which accommodates unfavorable noise conditions, template mismatch, and detector artifacts.

The followup code was verified to recover $95 \%$ of injections at or above the upper limit level for a uniform distribution of injection frequencies. (Figure 22).

The recovery criteria require that an outlier close to the true injection location (within 2 mHz in frequency $f$, $3 \times 10^{-10} \mathrm{~Hz} / \mathrm{s}$ in spindown and $12 \mathrm{rad} \cdot \mathrm{Hz} / f$ in sky location) be found and successfully pass through all stages of the detection pipeline. As each stage of the pipeline passes only outliers with an increase in SNR, this resulted in simulated outliers that stood out strongly above the


FIG. 2. PowerFlux injection recovery. The injections were performed in the $50-200 \mathrm{~Hz}$ band. The injected strain divided by the upper limit in this band (before injection) is shown on the horizontal axis. The percentage of surviving injections is shown on the vertical axis, with a horizontal line drawn at the $95 \%$ level. Stage 0 is the output of the coincidence test after the initial semi-coherent search. (color online).
background, with good estimates of the parameters of the underlying signals.

## B. FrequencyHough search method

The FrequencyHough method is described in detail in [23, 37, 38]. Calibrated detector data is used to create SFTs with coherence time depending on the frequency band being considered, see Table II Short timedomain disturbance are removed from the data before constructing the SFTs 39. A time-frequency map, called a peakmap, is built by selecting the local maxima (called peaks) over a threshold of 1.58 on the square root of the equalized power $\mathcal{R}(i)=\sqrt{\mathcal{P}(i) / S_{\mathrm{AR}}(i)}$, being $\mathcal{P}(i)$ the value of the periodogram of the data at the frequency index $i$, and $S_{\mathrm{AR}}(i)$ an auto-regressive estimation of the average power spectrum at the same frequency index [39] (then the index $i$ runs along the full frequency band being considered). The peakmap is cleaned using a line "persistency" veto, described in [38, which consists of projecting the peakmap onto the frequency axis and removing the frequency bins in which the projection is higher than a given threshold.

After defining a grid in the sky, the peakmap for each sky position is corrected for the Doppler effect caused by the detector motion by shifting each peak to compensate for this effect. Shifted peaks are then fed to the FrequencyHough algorithm, transforming each peak
to the frequency/spin-down plane of the source. The FrequencyHough algorithm is a particular implementation of the Hough transform, which is a robust parameter estimator of patterns in images. The frequency and spin-down bins depend on the frequency band, as indicated in Tab. II. The transformation properly weights any noise non-stationarity and the time-varying detector response [40].

The computation of the FrequencyHough transform is the most computationally demanding part of the analysis and needs to be split into thousands of independent jobs, each computing a FrequencyHough transform covering a small portion of the parameter space. In practice, each job covers 1 Hz , a small sky region-with a frequencydependent size such that jobs at lower frequencies cover larger regions - and a range of spin-down values, as detailed below. The output of a FrequencyHough transform is a 2-D histogram in the frequency/spin-down plane of the source.

For each FrequencyHough histogram, candidates for each sky location are selected by dividing the $1-\mathrm{Hz}$ band into 20 intervals and taking the most or (in most cases) the two most significant candidates for each interval, on the basis of the histogram number count. This is an effective procedure to avoid blinding by large disturbances in the data, which would contribute a large number of candidates if we used a toplist, i.e. if only candidates globally corresponding to the highest number count were selected. All the steps described thus far are applied separately to the data of each detector involved in the analysis.

Candidates from each detector are clustered and coincidence tests are applied between the two sets of clusters, using a distance metric built in the four-dimensional parameter space of position $(\lambda, \beta)$ (in ecliptical coordinates), frequency $f$ and spin-down $\dot{f}$, defined as

$$
\begin{equation*}
d_{\mathrm{FH}}=\sqrt{\left(\frac{\Delta f}{\delta f}\right)^{2}+\left(\frac{\Delta \dot{f}}{\delta \dot{f}}\right)^{2}+\left(\frac{\Delta \lambda}{\delta \lambda}\right)^{2}+\left(\frac{\Delta \beta}{\delta \beta}\right)^{2}} \tag{4}
\end{equation*}
$$

where $\Delta f, \Delta \dot{f}, \Delta \lambda$, and $\Delta \beta$ are the differences, for each parameter, among pairs of candidates of the two detectors, and $\delta f, \delta \dot{f}, \delta \lambda$, and $\delta \beta$ are the corresponding bins, that is the step width in a given parameter grid. Candidates within $d_{\mathrm{FH}}=3$ are considered coincident. Coincident candidates are subject to a ranking procedure, based on the value of a statistic built using the distance and the FrequencyHough histogram weighted number count of the coincident candidates. More precisely, let us indicate with $N$ the total number of coincident candidates in each $0.1-\mathrm{Hz}$ band. First, candidates are ordered in descending order of the number count, separately for each dataset, and a rank $r_{i, j}$ is assigned to each of them, from $1 / N$ to the highest to 1 to the smallest, where $i=1,2$ identifies the dataset and $j$ runs over the coincident candidates of a given dataset in a given $0.1-\mathrm{Hz}$ band. Then, coincident candidates are ordered in ascending order of

| Band $[\mathrm{Hz}]$ | Time duration $[\mathrm{s}]$ | $\delta f[\mathrm{~Hz}]$ | $\delta \dot{f}[\mathrm{~Hz} / \mathrm{s}]$ |
| :---: | :---: | :---: | :---: |
| $[20-128]$ | 8192 | $1.22 \cdot 10^{-4}$ | $1.18 \cdot 10^{-11}$ |
| $[128-512]$ | 4096 | $2.44 \cdot 10^{-4}$ | $2.36 \cdot 10^{-11}$ |
| $[512-1024]$ | 2048 | $4.88 \cdot 10^{-4}$ | $4.71 \cdot 10^{-11}$ |
| $[1024-2048]$ | 1024 | $9.76 \cdot 10^{-4}$ | $9.42 \cdot 10^{-11}$ |

TABLE II. Properties of the FFTs used in the FrequencyHough pipeline. The time duration refers to the length in seconds of the data chunks on which the FFT is computed. The frequency bin width is the inverse of the time duration, while the spin-down bin width is computed as $\delta \dot{f}=\delta f / T_{\text {obs }}$. In the analysis described in this paper only the first two bands have been considered.
their distance, and a rank $r_{d, j}$ is assigned to each pair, going from $1 / N$ for the nearest to 1 for the farthest. A final rank $r_{j}=r_{d, j} \times \prod_{i=1}^{2} r_{i, j}$ is computed and will take smaller values for more significant candidates, i.e. having smaller distance and higher number counts. A number of the most significant candidates are selected for each $0.1-\mathrm{Hz}$ band and are subject to a follow-up procedure in order to confirm or reject them. This number depends on the amount of computing power which can be devoted to the follow-up. For the analysis described in this paper 4 candidates have been selected in each $0.1-\mathrm{Hz}$ band.

## 1. Candidate follow-up

The follow-up consists of several steps (a detailed description is given in [23]). First, for each candidate, a fully coherent search using data from both detectors is performed assuming the parameters found for the candidate in this analysis. Although the coherent search corrects exactly for the Doppler and spin-effect at a single particular point in the parameter space, corresponding to the candidate, the correction is extended, by linear interpolation, to the neighbors of the candidate. In practice, this means that from the resulting corrected and downsampled time series, a new set of longer SFTs can be built, by a factor of 10 in this analysis, as well as a set of new (Doppler corrected) peakmaps. The new peakmaps are valid even if the true signal parameters are slightly different from those of the candidate under consideration.

The joint corrected peakmaps (individually corrected for each detector's motion) are input to the FrequencyHough algorithm: overall, 1681 transforms are computed, covering $\pm 50 \mathrm{mHz}, \pm 1$ spindown bins (of initial width) and $\pm 0.75$ bins (of initial width) for both $\lambda$ and $\beta$ around the candidate and the loudest candidate among the full set of FrequencyHough maps is selected (note that the bin widths are now 10 times smaller than those of the initial stage of the analysis). The starting peakmap is then corrected using the parameters of the loudest candidate and projected on the frequency axis. We take the maximum of this projection in a range of $\pm 2$ bins (of initial width) around the candidate frequency. We divide the rest of the $0.1-\mathrm{Hz}$ band (which we consider the "off-source" region) into $\sim 200$ intervals of the same width, take the maximum
of the peakmap projection in each of these intervals and sort in decreasing order all these maxima. We tag the candidate as "interesting" if it ranks first or second in this list.

Those candidates passing these tests are subject to further analysis: those candidates coincident with known noise lines (and that survived previous cleaning steps) are discarded, candidates with multi-interferometer significance less than the single-interferometer significance are discarded, candidates with single-interferometer significances differing by more than a factor of five are discarded, or candidates that have single-interferometer critical ratios $\left(\mathrm{CR}=\left(A_{p}-\mu_{p}\right) / \sigma_{p}\right.$, being $A_{p}$ the candidate projection amplitude, $\mu_{p}$ and $\sigma_{p}$ the mean and standard deviation of the projection) differing by more than a factor of five are discarded. The choice of this factor is a conservative one, validated by simulations, such that a detectable signal would not be vetoed at this stage. The outliers passing also these steps are subject to additional, manual scrutiny, see Sec. V Cfor more details concerning the O1 outliers.

As a validation of the follow-up we have made a study of software injection recovery. Specifically, we have generated about 110 signals which have been injected into representative $1-\mathrm{Hz}$ bands, $64-65 \mathrm{~Hz}$ and $122-123 \mathrm{~Hz}$, following the procedure described at the beginning of Sec. IV B 2 and with amplitude equal to the upper limit computed in those bands. The data has been analyzed with the FrequencyHough pipeline and candidates selected, as discussed in Sec. IVB. These candidates have been subject to the follow-up and all the candidates due to injected signals, i.e. within the standard follow-up volume around the corresponding injection, have been confirmed, showing a CR $>11$ (to be compared with 7.57 which is the threshold used in the real analysis to select outliers, see Sec. V C). Moreover, we have verified that in most cases (about $90 \%$ of the cases in this test) the followup allows to improve parameter estimation. In Figs. 3, 4 we show the a-dimensional distance of candidates associated to simulated signals from their injection, defined by Eq. 4 both before and after the follow-up. The median of the distance reduces from 1.62 to 0.85 for the first band and from 1.55 to 0.88 for the second.


FIG. 3. A-dimensional distance between 56 injected signals in the band $64-65 \mathrm{~Hz}$ and the corresponding candidates (blue dots: before the follow-up; red circles: after the follow-up).


FIG. 4. A-dimensional distance between 57 injected signals in the band $122-123 \mathrm{~Hz}$ and the corresponding candidates (blue dots: before the follow-up; red circles: after the follow-up).

## 2. Upper limit computation

Upper limits are computed in each $1-\mathrm{Hz}$ band between 20 Hz and 475 Hz by injecting software simulated signals, with the same procedure used in [23]. For each 1 Hz band 20 sets of 100 signals each are generated, with fixed amplitude within each set and random parameters (sky location, frequency, spin-down, and polarization parameters). These are complex signals generated in the time domain at a reduced sampling frequency of 1 Hz , and then added to the data of both detectors in the frequency domain. For each injected signal in a set of 100 , an analysis is done using the FrequencyHough pipeline over a frequency band of 0.1 Hz around the injection frequency, the full spin-down range used in the real analysis, and nine sky points around the injection position [23]. Candidates are selected exactly as in the real analysis, but no clustering is applied because it would be affected by the presence of too many signals. Then, coincidences are required directly among candidates (clustering has been used mainly to reduce computational cost). Coincident candidates that are within the follow-up volume around the injection parameters, and that have a critical ratio larger than the largest critical ratio found in the real analysis in the same band are considered as "detections"
(excluding those that fall in a frequency bin vetoed by the persistency veto).

The upper limit in a given 1 Hz band is given by the signal amplitude such that $95 \%$ of the injected signals are detected. In practice, typically, a fit is used to the measured detection efficiency values in order to interpolate the detection efficiency when injections do not cover densely enough the $95 \%$ region. The fit has been done with the cumulative of a modified Weibull distribution function, given by

$$
\begin{equation*}
D(x)=K\left(1-e^{-A_{1}\left(x-x_{\min }\right)^{A_{2}}}\right) \tag{5}
\end{equation*}
$$

where $x=\log _{10}\left(h_{\mathrm{inj}}\right), h_{\mathrm{inj}}$ is the injected amplitude, $x_{\text {min }}$ is the value such that $D\left(x_{\min }\right)=0, K$ is a scaling factor such that the maximum of $D(x)$ is equal to the maximum measured detection efficiency, and $A_{1}$ and $A_{2}$ are the fit parameters. As an example, in Figure 5 the measured detection efficiency values for the band $423-424 \mathrm{~Hz}$ are shown together with the fit. In cases like this, corresponding to artifact-free bands, the fit is accurate.


FIG. 5. Measured detection efficiency values for the band $423-424 \mathrm{~Hz}$ (circles) and their fit done using Eq. 5 (asterisks). The dashed line represents the full fitted curve. The dotted horizontal line indicates the $95 \%$ level of the detection efficiency.

In more disturbed bands, the fit is not able to closely follow the measured values, as shown, for example, in Figure 6 In such cases, if an interpolation is needed, a linear interpolation is used between the two detection efficiency points nearest (one from below and one from above) to the $95 \%$ level.

## C. SkyHough search method

The SkyHough search method is described in detail in [18, 4143]. Calibrated detector $h(t)$ data from the O1 run is used to create 1800-s Tukey-windowed SFTs, where each SFT is created from a segment of detector data that is at least 1800 s long. From this step, 3684


FIG. 6. Measured detection efficiency values for the band 5152 Hz (circles) and their fit done using Eq. 5 (asterisks). The dashed line represents the full fitted curve. The dotted horizontal line indicates the $95 \%$ level of the detection efficiency.
and 3007 SFTs are created for H 1 and L1, respectively. The data from the two LIGO interferometers are initially analyzed in separate all-sky searches for continuous gravitational wave signals, and then coincidence requirements on candidates are imposed.

SFT data from a single interferometer is analyzed by creating a peak-gram (a collection of zeros and ones) by setting a threshold of 1.6 on their normalized power. This is similar to the FrequencyHough method, but, in this case, the averaged spectrum is determined via a runningmedian estimation [12].

An implementation of the weighted Hough transform [18, 42] is used to map points from the timefrequency plane of the peak-grams into the space of the source parameters. Similar to the methods described previously, the algorithm searches for signals whose frequency evolution fits the pattern produced by the Doppler shift and spindown in the time-frequency plane of the data. In this case, the Hough number count is the weighted sum of the ones and zeroes, $n_{k}^{(i)}$, of the different peak-grams along the track corresponding to each point in parameter space. This sum is computed as

$$
\begin{equation*}
n=\sum_{i=0}^{N-1} w_{k}^{(i)} n_{k}^{(i)} \tag{6}
\end{equation*}
$$

where the choice of weights is optimal 42. These weights are given by

$$
\begin{equation*}
w_{k}^{(i)} \propto \frac{1}{S_{k}^{(i)}}\left\{\left(F_{+1 / 2}^{(i)}\right)^{2}+\left(F_{\times 1 / 2}^{(i)}\right)^{2}\right\} \tag{7}
\end{equation*}
$$

where $F_{+1 / 2}^{(i)}$ and $F_{\times 1 / 2}^{(i)}$ are the values of the antenna pattern functions at the mid-point of the $i^{\text {th }}$ SFT for the sky location of interest and $S_{k}^{(i)}$ is the SFT noise level. A particularly useful detection statistic is the significance
(or critical ratio), and is given by

$$
\begin{equation*}
s=\frac{n-\langle n\rangle}{\sigma}, \tag{8}
\end{equation*}
$$

where $\langle n\rangle$ and $\sigma$ are the expected mean and standard deviation of the Hough number count for pure noise.

The SkyHough search analyzes $0.1-\mathrm{Hz}$ bands over the frequency interval $50-500 \mathrm{~Hz}$, frequency time derivatives in the range $[-1.0,+0.1] \times 10^{-8} \mathrm{~Hz} / \mathrm{s}$, and covering the entire sky. A uniform grid spacing, equal to the size of a SFT frequency bin, $\delta f=1 / T_{\text {coh }}=5.556 \times 10^{-4} \mathrm{~Hz}$ is chosen, where $T_{\text {coh }}$ is the duration of an SFT. The resolution $\delta \dot{f}$ is given by the smallest value of $\dot{f}$ for which the intrinsic signal frequency does not drift by more than one frequency bin during the total observation time $T_{\text {obs }}$ : $\delta \dot{f}=\delta f / T_{\text {obs }} \sim 4.95 \times 10^{-11} \mathrm{~Hz} \mathrm{~s}^{-1}$. This yields 224 spindown values for each frequency. The sky resolution, $\delta \theta$ is frequency dependent, with the number of templates increasing with frequency, as given by Eq.(4.14) of Ref. 41, using a pixel-factor of $N_{p}=2$ :

$$
\begin{equation*}
\delta \theta=\frac{10^{4} \delta f}{f N_{p}} \tag{9}
\end{equation*}
$$

For each frequency band, the parameter space is split further into 209 sub-regions of the sky. For every sky region and frequency band the analysis program compiles a list of the 1000 most significant candidates. A final list of the 1000 most significant candidates per frequency band is constructed, with no more than 300 candidates from a single sky region. This procedure reduces the influence of instrumental spectral disturbances that affect specific sky regions.

The post-processing of the results for each $0.1-\mathrm{Hz}$ band consists of the following steps:
(i) Apply a $\chi^{2}$ test, as described below, to eliminate candidates caused by detector artifacts.
(ii) Search for coincident candidates among the two data sets, using a coincidence window of $d_{\mathrm{SH}}<\sqrt{14}$. This dimensionless quantity, similar to the parameter $d_{\mathrm{FH}}$ used in the FrequencyHough pipeline, is defined as:

$$
\begin{equation*}
d_{\mathrm{SH}}=\sqrt{(\Delta f / \delta f)^{2}+(\Delta \dot{f} / \delta \dot{f})^{2}+(\Delta \theta / \delta \theta)^{2}} \tag{10}
\end{equation*}
$$

to take into account the distances in frequency, spin-down and sky location with respect to the grid resolution in parameter space. Here, $\Delta \theta$ is the sky angle separation. Each coincidence pair is then characterized by its harmonic mean significance value and a center in parameter space: the mean weighted value of frequency, spin-down and sky-location obtained by using their corresponding individual significance values. Subsequently, a list containing the 1000 most significant coincident pairs is produced for each $0.1-\mathrm{Hz}$ band.
(iii) The surviving coincidence pairs are clustered, using the same coincidence window of $d_{\mathrm{SH}}=\sqrt{14}$ applied to the coincidence centers. Each coincident candidate
can belong to only a single cluster, and an element belongs to a cluster if there exists at least another element within that distance. Only the highest ranked cluster, if any, will be selected for each $0.1-\mathrm{Hz}$ band. Clusters are ranked based on their mean significance value, but where all clusters overlapping with a known instrumental line are ranked below any cluster with no overlap. A cluster is always selected for each of the $0.1-\mathrm{Hz}$ bands that had coincidence candidates. In most cases the cluster with the largest mean significance value coincides also with the one containing the highest value.

Steps (ii) and (iii) take into account the possibility of coincidences and formation of clusters across boundaries of consecutive $0.1-\mathrm{Hz}$ frequency bands. The following tests are performed on those candidates remaining:
(iv) Based on previous studies [26], we require that interesting clusters must have a minimum population of 6 and that coincidence pairs should be generated from at least 2 different candidates per detector.
(v) For those candidates remaining, a multi-detector search is performed to verify the consistency of a possible signal. Any candidate that has a combined significance more than 1.6 below the expected value is discarded.

Outliers that pass these tests are manually examined. In particular, outliers are also discarded if the frequency span of the cluster coincides with the list of narrow instrumental lines described in Sec. II, or if there are obvious spectral disturbances associated with one of the detectors.

$$
\text { 1. The } \chi^{2} \text { veto }
$$

The $\chi^{2}$-test was first implemented in the SkyHough analysis of initial LIGO era S5 data [18, and is used to reduce the number of candidates from single interferometer analysis before the coincidence step. A veto threshold for the $\chi^{2}$-test is derived empirically from the O1 SFT data set. A large number of simulated periodic gravitational wave signals are added to the SFTs, with randomly chosen amplitude, frequency, frequency derivative, sky location, polarization angle, inclination angle, and initial phase. Then the data is analyzed separately for each detector, H1 and L1.

To determine the $\chi^{2}$ veto threshold (characterized by a "veto curve"), $1250.1-\mathrm{Hz}$ bands are selected for H1 and 107 bands for L1, bands free of known large spectral disturbances. In total 2,340,000 injections are analyzed. The $\chi^{2}$ values are defined with respect to a split of the SFT data into $p=16$ segments. The results are sorted with respect to the significance and grouped in sets containing 2000 points. For each set the mean value of the significance, the mean of the $\chi^{2}$, and its standard deviation are computed. With this reduced set of points, we fit two power laws $p-1+A_{1} s^{A_{2}}$ and $\sqrt{2 p-2}+B_{1} s^{B_{2}}$ to the mean and standard deviation curve.

A detailed study of the calibration of the $\chi^{2}$ test using LIGO O1 data can be found in [44]. This study revealed a
frequency-dependent behavior. In particular, the results obtained from injections below 100 Hz differ from those between 100 and 200 Hz , while the characterization of the $\chi^{2}$-significance plane was similar for frequencies higher than 200 Hz . For this reason, three different veto curves have been derived for the $50-100 \mathrm{~Hz}$ band, $100-200 \mathrm{~Hz}$ band, and for frequencies higher than 200 Hz . In the corresponding frequency bands, the characterization was similar for both interferometers. Therefore, common veto curves are derived.

| $f[\mathrm{~Hz}]$ | $A_{1}$ | $A_{2}$ | $B_{1}$ | $B_{2}$ |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| $50-100$ | 0.4902 | 1.414 | 0.3581 | 1.481 |
| $100-200$ | 0.2168 | 1.428 | 0.1902 | 1.499 |
| $>200$ | 0.1187 | 1.470 | 0.0678 | 1.697 |

TABLE III. Parameters obtained for the O1 $\chi^{2}$ veto curve characterization in different frequency bands

The coefficients obtained for the proposed characterization can be found in Table IIT Figures 7, 8, and 9 show the fitted curves and resulting veto curves corresponding veto for the mean $\chi^{2}$ plus five times its standard deviation for the H1-L1 combined data. The associated falsedismissal rate for this veto is measured to be $0.12 \%$ for the $50-100 \mathrm{~Hz}$ band, $0.21 \%$ for the $100-200 \mathrm{~Hz}$ band, and $0.16 \%$ for frequencies higher than 200 Hz .


FIG. 7. Significance- $\chi^{2}$ plane for 180000 simulated injected signals in the 50 to 100 Hz band together with the fitted mean curve (dot-dashed line) and the veto curve (dashed line) corresponding to the mean $\chi^{2}$ plus five times its standard deviation for the H1-L1 combined data. The associated false dismissal rate (percentage of injections that are higher than the veto curve) is measured to be $0.12 \%$


FIG. 8. Same as Fig. 7 for 320000 injections in the 100 to 200 Hz band. The false dismissal rate being $0.21 \%$


FIG. 9. Same as Fig. 7 for 1840000 injections at frequencies higher than 200 Hz for the combined H1-L1 data. The false dismissal rate being $0.16 \%$

## 2. The multi-detector consistency veto

Similar to the preceding $\chi^{2}$ test, a multi-detector consistency veto can be derived by comparing the significance results from a multi-detector search to those obtained by analyzing the data from the H 1 and L 1 detectors separately.

In particular, for each point in parameter space, we can derive the expected multi-detector significance from the significance obtained in the separate analysis of H1 and L1 data by using the weights defined by Eqn. 7 and the SFT sets in use. Since in this search the exact value of the weights is not stored, an approximation can be derived by ignoring the effect of the antenna pattern and considering only the influence of the varying noise levels of the different SFTs in a given frequency band.

The following expression can then be derived for the
multi-detector search

$$
\begin{equation*}
s_{\text {theo }}=\frac{s_{\mathrm{L} 1} \sqrt{\sum_{i=0}^{N_{\mathrm{L} 1}}\left(S_{\mathrm{L} 1}^{(i)}\right)^{-2}}+s_{H 1} \sqrt{\sum_{i=0}^{N_{\mathrm{H} 1}}\left(S_{\mathrm{H} 1}^{(i)}\right)^{-2}}}{\sqrt{\sum_{i=0}^{N_{\mathrm{L} 1}}\left(S_{\mathrm{L} 1}^{(i)}\right)^{-2}+\sum_{i=0}^{N_{\mathrm{H} 1}}\left(S_{\mathrm{H} 1}^{(i)}\right)^{-2}}} \tag{11}
\end{equation*}
$$

where $N_{\mathrm{H} 1}$ and $N_{\mathrm{L} 1}$ are the number of SFTs of each detector, $S_{\mathrm{H} 1}^{(i)}$ and $S_{\mathrm{L} 1}^{(i)}$ are the one-sided PSDs of each detector averaged around a small frequency interval, and $s_{\mathrm{H} 1}$ and $s_{\mathrm{L} 1}$ are the significances of the separate singledetector searches.

Ideally, a coincidence pair from a periodic gravitational wave signal would have $s_{\mathrm{H} 1}, s_{\mathrm{L} 1}$, and $s_{\text {theo }}$ values consistent with Eq. 11 within uncertainties arising from use of nearby-but not identical-templates and from noise fluctuations. Furthermore, we are interested in characterizing its validity when considering the maximum significance values obtained in a small volume in parameter space.

In order to test the validity of the consistency requirement, we have injected simulated signals in the 50-500 Hz range, randomly covering the same parameters of our search and for a variety of signal amplitudes. A full search, but covering only one sky patch, is performed on H1 and L1 data, as well as for the combined SFT data, returning a list of the most significant candidates for each of them. Of all the injections performed, we considered only those with amplitudes strong enough that within a frequency and spin-down window of 4 bins around the injected signal parameters, the maximum significance value would be at least 5 for both individual single interferometer searches, and consequently a theoretical combined significance higher than 7. A total of 4356 injections with an expected theoretical combined significance between 7 and 50 were considered, and the results are presented in Figure 10

In Figure 10 we characterize the difference in significance obtained with respect to the theoretical expected value. From this plot, the multi-detector consistency veto for the O1 data used in this search can be determined: if the multi-detector combined significance has a value more than 1.6 below the nominal theoretically expected value, the candidate is vetoed. This value of 1.6 yields a false dismissal rate of $0.07 \%$.

## 3. Upper limit computation

Upper limits are derived from the sensitivity depth for each $0.1-\mathrm{Hz}$ band between 50 and 500 Hz . The value of the depth corresponding to the averaged $95 \%$ confidence level upper limit is obtained by means of simulated periodic gravitational wave signals added into the SFT data of both detectors H1 and L1 in a limited number of frequency bands. In those bands, the detection efficiency, i.e., the fraction of signals that are considered detected (that have passed steps (i)-(iv) above), is computed as a


FIG. 10. Characterization of the multi-detector significance consistency veto using 4356 simulated injected signals in the $50-500 \mathrm{~Hz}$ range. Each point represents a separate injection. The horizontal axis corresponds to the theoretical expected significance value, $s_{\text {theo }}$, while the vertical axis is the difference between the theoretical and the measured value of significance, $s_{m u l t i}^{*}$. The solid line is placed at a difference in significance of 1.6 that has only been exceeded by 3 injections.
function of signal strength, $h_{0}$ expressed by the sensitivity depth $\sqrt{S_{n}} / h_{0}(1 / \sqrt{\mathrm{Hz}})$. Here, $S_{n}$ is the maximum over both detectors of the power spectral density of the data, at the frequency of the signal, estimated as the power-2 mean value, $\left(\sum_{i=1}^{N}\left(S_{k}^{(i)}\right)^{-2} / N\right)^{-2}$, across the different noise level $S_{k}^{(i)}$ of the different $N$ SFTs.


FIG. 11. Detection efficiency as a function of depth obtained for 22 frequency bands. Each dot corresponds to a set of 200 signal injections. The solid line (red) correspond to the fitted sigmoid curve. The diamond shows the depth value corresponding to an averaged all-sky $95 \%$ detection efficiency, $D^{95 \%}=24.2(1 / \sqrt{\mathrm{Hz}})$.

Twenty-two different $0.1-\mathrm{Hz}$ bands free of spectral disturbances in both detectors were selected with the following starting frequencies $[73.6,80.8,98.3,140.8,170.2$, 177.8 , 201.1, 215.1, 240.7, 240.8, 250.7, 305.3, 320.3, $350.6,381.6,400.7,402.1,406.8,416.2,436.9,446.9$, 449.4]. In all these selected bands, we generated five sets of 200 signals each, with fixed sensitivity depth each set and random parameters $\left(f, \alpha, \delta, \dot{f}, \varphi_{0}, \psi, \cos \iota\right)$. For each injected signal added into the data of both detectors an analysis was done using the SkyHough search pipeline over a frequency band of 0.1 Hz and the full spindown range, but covering only one sky patch. For this sky-patch a list of 300 loudest candidates was produced. Then we imposed a threshold on significance, based on the minimum significance found in the all-sky search in the corresponding $0.1-\mathrm{Hz}$ band before any injections. The post-processing is then done using the same parameters as in the search, including the population veto.

For each of those 22 frequency bands, a sigmoid curve,

$$
\begin{equation*}
\operatorname{Efficiency}(\text { Depth })=1-\frac{1}{1+\exp (b(\text { Depth }-a))}, \tag{12}
\end{equation*}
$$

was fitted by means of the least absolute residuals. Then the $95 \%$ confidence upper limit was deduced from the corresponding value of the depth. With this procedure, the minimum and maximum values of the depth corresponding to the desired upper limit were 21.9 and $26.6(1 / \sqrt{\mathrm{Hz}})$ respectively. We also collected the results from all the frequency bands and, as shown in Figure 11, performed a sigmoid fitting as before and obtained the following fitted coefficients (with $95 \%$ confidence bounds): $a=39.83(34.93,44.73)(1 / \sqrt{\mathrm{Hz}})$ and $b=-0.1882(-0.2476,-0.1289)(\sqrt{\mathrm{Hz}})$, that yields the joint depth for corresponding to the $95 \%$ upper limit of $D^{95 \%}=24.2(1 / \sqrt{\mathrm{Hz}})$, its uncertainty being smaller than $7 \%$ for undisturbed bands, with the exception of the 98.3 Hz band for which the upper limit using this joint value would be underestimated by $10 \%$ and for 406.8 Hz band for which the upper limit is overestimated by $9.5 \%$.

The $95 \%$ confidence upper limit on $h_{0}$ for undisturbed bands can then be derived by simply scaling the power spectral density of the data, $h_{0}^{95 \%}=\sqrt{S_{n}} / D^{95 \%}$. The computed upper limits are shown in Figure 12. No limits have been placed in $1940.1-\mathrm{Hz}$ bands in which coincidence candidates were detected, as this scaling procedure can have larger errors in those bands due to the presence of spectral disturbances.

## D. Time-Domain $\mathcal{F}$-statistic search method

The Time-Domain $\mathcal{F}$-statistic search method uses the algorithms described in [19, 27, 45, 46] and has been applied to an all-sky search of VSR1 data 19 .

The search method consists primarily of two parts. The first part is the coherent search of narrowband, timedomain segments. The second part is the search for co-


FIG. 12. SkyHough O1 upper limits. The dotted (red) curve shows the averaged $95 \%$ confidence level upper limits for every analyzed $0.1-\mathrm{Hz}$ band. The vertical (grey) lines indicate $1940.1-\mathrm{Hz}$ bands in which coincidence candidates were found and consequently no upper limits are set.
incidences among the candidates obtained from the coherent search (see Figure 13).

The time-domain segments of the data are extracted from the same set of SFTs used by the FrequencyHough pipeline. The data are split into bands of 0.25 Hz long. The bands are overlapped by $2 \times 10^{-7} \mathrm{~Hz}$. For each band, the data is inverse Fourier transformed to extract a time series of O1 data from the SFTs. The time series is divided into segments, called frames, of six sidereal days long each. Thus, the band [10-475] Hz has 1921 frequency bands. The band number $b$ is related to the reference band frequency $f_{b}$ as follows:

$$
\begin{equation*}
f_{b}=10 \mathrm{~Hz}+\frac{b\left(1-2^{-5}\right)}{2 \Delta t} \tag{13}
\end{equation*}
$$

where the sampling time $\Delta t=2 \mathrm{~s}$. For O1 data, which is about 120 days long, we obtain 20 time frames. Each 6 -day narrowband segment contains $N=258492$ data points. The O1 data has a number of non-science data segments. The values of these bad data are set to zero. For analysis, we choose only segments that have a fraction of bad data less than $1 / 3$. This requirement results in eight 6 -day-long data segments for each band. Consequently, we have 15368 data segments to analyze. These segments are analyzed coherently using the $\mathcal{F}$-statistic.

We set a fixed threshold for the $\mathcal{F}$-statistic of $\mathcal{F}_{0}=14.5$ and record parameters of all the threshold crossings together with the corresponding values of the signal-tonoise ratio $\rho$

$$
\begin{equation*}
\rho=\sqrt{2(\mathcal{F}-2)} \tag{14}
\end{equation*}
$$

For the search we use a four-dimensional (parametrized by frequency, spindown, and two more parameters related to the position of the source in the sky) grid of templates constructed in Sec. 4 of [46, which belongs to the family $S_{1}$ of grids considered in 46. The grid has a minimal match $\mathrm{MM}=\sqrt{3} / 2$ and its thickness equals 1.77959, what is only $\sim 0.8 \%$ larger than the thickness of the four-dimensional optimal lattice covering $A_{4}^{*}$ (equal to 1.76553 ). We also veto candidates overlapping with lines identified as instrumental artifacts.

In the second stage of the search we search for coincidences among the candidates obtained in the coherent part of the search. We use exactly the same coincidence search algorithm as in the analysis of VSR1 data and described in detail in Section 8 of [19]. We search for coincidences in each of the 1921 bands analyzed. To estimate the significance of a given coincidence, we use the formula for the false alarm probability derived in the appendix of [19]. Sufficiently significant coincidences are


FIG. 13. Time-Domain $\mathcal{F}$-statistic pipeline flowchart. Two main parts of the pipeline are the coherent $\mathcal{F}$-statistic search for candidate signals in time-domain segments, which is followed by a search for coincidences between candidates from different time-domain segments.
called outliers and subject to further investigation.

## 1. Sensitivity of the search

The sensitivity of the search is taken to be the amplitude $h_{0}$ of the gravitational wave signal that can be confidently detected. To estimate the sensitivity we use a procedure developed in [13]. We determine the sensitivity of the search in each of the 1921 frequency bands that we have searched. We perform Monte-Carlo simulations in which, for a given amplitude $h_{0}$, we randomly select the other seven parameters of the signal: $\omega_{0}, \omega_{1}, \alpha, \delta, \phi_{0}, \iota$ and $\psi$. We choose frequency and spindown parameters uniformly over their range, and source positions uniformly over the sky. We choose angles $\phi_{0}$ and $\psi$ uniformly over the interval $[0,2 \pi]$ and $\cos \iota$ uniformly over the interval $[-1,1]$. For each band, the simulated signal is added to all the data segments chosen for the analysis in that band. Then the data is processed through the pipeline.

First, we perform a coherent $\mathcal{F}$-statistic search of each of the data segments where the signal was added, and store all the candidates above a chosen $\mathcal{F}$-statistic thresh-


FIG. 14. Time-Domain $\mathcal{F}$-statistic method of establishing upper limits from the Monte-Carlo simulations with sigmoid fitting (an example for band no. 0666). Blue dots denote the results of the MC simulations for the range of amplitudes $h_{0}$ of injected signals with otherwise randomly chosen parameters. The green curve is the best fit of Eq. 15 the red dot corresponds to the $95 \%$ upper limit (see Figure 18 for the summary of results for the whole range of searched frequencies).
old of 14.5. In this coherent analysis, to make the computation manageable, we search over a limited parameter space consisting of $\pm 2$ grid points around the nearest grid point where the signal was added. Then the coincidence analysis of the candidates is performed. The signal is considered to be detected, if it is coincident in more than 5 of the 8 time frames analyzed for a given band. The ratio of numbers of cases in which the signal is detected to the total number of simulations performed for a given $h_{0}$ determines the frequentist sensitivity upper limits. To obtain the $95 \%$ confidence sensitivity limit on $h_{0}$ we fit a sigmoid function,

$$
\begin{equation*}
S(x)=\frac{1}{1+e^{k\left(x_{0}-x\right)}} \tag{15}
\end{equation*}
$$

to these data, with $x_{0}$ and $k$ being the fitted parameters. An example result, for a band frequency 171.296875 Hz (corresponding to band number 0666) is presented in Figure 14 . The $95 \%$ confidence upper limits for the whole range of frequencies are given in Figure 18, they follow very well the noise curves of the O1 data that were analyzed.

## V. SEARCH RESULTS

## A. Introduction

Results from the four search pipelines are presented below. In summary, no pipelines found a credible gravitational wave signal after following up initial outlier can-
didates, and each pipeline obtained a set of upper limits. In a number of bands, particularly at low frequencies, instrumental artifacts prevented setting of reliable upper limits. The sensitivities obtained by the different pipelines are comparable and generally in line with expectations from the previous mock data challenge that used data from the Initial LIGO S6 run [26], but a greater density of instrumental artifacts in the O1 data and refined algorithm parameter choices led to additional small performance differences in this analysis. In addition to the upper limits graphs presented below, numerical data for these values can be obtained separately 47.

## B. PowerFlux search results

The PowerFlux algorithm and Loosely Coherent method compute power estimates for continuous gravitational waves in a given frequency band for a fixed set of templates. The template parameters usually include frequency, first frequency derivative and sky location.

Since the search target is a rare monochromatic signal, it would contribute excess power to one of the frequency bins after demodulation. The upper limit on the maximum excess relative to the nearby power values can then be established. For this analysis we use a universal statistic [25] that places conservative $95 \%$ confidence level upper limits for an arbitrary statistical distribution of noise power. The universal statistic has been designed to provide close to optimal values in the common case of Gaussian distribution.

The upper limits obtained in the search are shown in Figure 15 . The upper (yellow) curve shows the upper limits for a worst-case (linear) polarization when the smallest amount of gravitational energy is emitted toward the Earth. The lower curve shows upper limits for an optimally oriented source (circular polarization). Because of the day-night variability of the interferometer sensitivity due to anthropogenic noise, the linearly polarized sources are more susceptible to detector artifacts, as the detector response to such sources varies with the same period.

Each point in Figure 15 represents a maximum over the sky, except for a small excluded portion of the sky near the ecliptic poles, which is highly susceptible to detector artifacts due to stationary frequency evolution produced by the combination of frequency derivative and Doppler shifts. The exclusion procedure is described in [16] and applied to $0.2 \%$ of the sky over the entire run.

If one assumes that the source spindown is solely due to emission of gravitational waves, then it is possible to recast upper limits on source amplitude as limits on source ellipticity. Figure 16 shows the reach of the PowerFlux search under different assumptions on source distance for circularly polarized signals. Superimposed are lines corresponding to sources of different ellipticities. Although not presented here, corresponding maximum ranges for circularly polarized sources derived from the strain upper limits of the other three pipelines would be similar.

The detection pipeline produced 62 outliers located near a $0.25-\mathrm{Hz}$ comb of detector artifacts (table X), 74 outliers spanning only one data segment (about 1 month) which are particularly susceptible to detector artifacts (table IX) and 25 outliers (table VIII) that do not fall into either of those two categories. Each outlier is identified by a numerical index. We report here SNR, frequency, spindown and sky location.

The "Segment" column describes the persistence of the outlier through the data, and specifies which contiguous subset of the three equal partitions of the timespan contributed most significantly to the outlier: see [22] for details. A true continuous signal from an isolated source would normally have $[0,2]$ in this column (similar contribution from all 3 segments), or on rare occasions $[0,1]$ or $[1,2]$. Any other range strongly suggests a statistical fluctuation, an artifact or a signal that does not conform to the phase evolution of Equation 2 .

During the O1 run several simulated pulsar signals were injected into the data by applying a small force to the interferometer mirrors with auxiliary lasers or via inductive forces from nearby electrodes 48. Several outliers were due to such hardware injections (Table IV). The hardware injection ip3 was exceptionally strong with a clear signature even in its non-Gaussian band. Note, however that these injections were not enabled for the H1 interferometer in the first part of the O1 run, leading to degraded efficiency for their detections.

The recovery of the hardware injections gives us additional confidence that no potential signals were missed. Manual followup has shown non-injection outliers spanning all three segments to be caused by pronounced detector artifacts. Several outliers (numbers 47, 56, 70, 72, 134, 138, 154 in table VIII spanning 2 segments were also investigated with a fully coherent followup based on the Einstein@Home pipeline [31, 32]. None was found to be consistent with the astrophysical signal model. Tables with more details may be found in Appendix A.

## C. FrequencyHough search results

In this section we report the main results of the O1 allsky search using the FrequencyHough pipeline. The number of initial candidates produced by the Hough transform stage was about $4.79 \cdot 10^{9}$ (of which about $2.58 \cdot 10^{8}$ belong to the band $20-128 \mathrm{~Hz}$, and the rest to the band $128-512 \mathrm{~Hz}$ ) for both Hanford and Livingston detectors. As the number of coincident candidates remained too large, 231475 for the band $20-128 \mathrm{~Hz}$ and 3109841 for the band $128-512 \mathrm{~Hz}$, we reduced it with the ranking procedure described in Sec. IV B. In practice, for computational efficiency reasons all the analysis was carried out separately for two different spin-down ranges: one from $+10^{-9} \mathrm{~Hz} / \mathrm{s}$ to $-2 \cdot 10^{-9} \mathrm{~Hz} / \mathrm{s}$ and the other from $-2 \cdot 10^{-9} \mathrm{~Hz} / \mathrm{s}$ to $-10^{-8} \mathrm{~Hz} / \mathrm{s}$. As a consequence, the number of candidates selected after the ranking was 8640 for the band $20-128 \mathrm{~Hz}$, and 30720 for the band $128-512 \mathrm{~Hz}$.


FIG. 15. PowerFlux O1 upper limits. The upper (yellow) curve shows worst-case (linearly polarized) 95\% CL upper limits in analyzed 62.5 mHz bands. The lower (grey) curve shows upper limits assuming a circularly polarized source. The data for this plot can be found in 47. (color online)

Each of these candidates was subject to the follow-up procedure, described in Sec. IV B 1. The number of candidates passing the first follow-up stage was 273 for the band $20-128 \mathrm{~Hz}$ and 1307 for the band $128-512 \mathrm{~Hz}$ and, after further vetoes, reduced to 64 for the band 20-128 Hz and 496 for the band $128-512 \mathrm{~Hz}$.

From these surviving candidates we selected the outliers less consistent with noise fluctuations. In particular, we chose those for which the final peakmap projection has a critical ratio $\mathrm{CR}>7.57$. This is the threshold corresponding to a false alarm probability of $1 \%$ on the noise-only distribution after having taken into account the look-elsewhere effect (on the follow-up stage) 49]. The list of outliers is shown in Tab. XI. Each of these outliers has been manually examined, and for all of them a gravitational wave origin could be excluded, as discussed in Appendix B

Upper limits have been computed in $1-\mathrm{Hz}$ bands, as described in IV B 2 and are shown in Figure 17. The minimum value is about $2.5 \cdot 10^{-25}$, reached in the range $150-200 \mathrm{~Hz}$. In a number of frequency bands the upper limit value deviates from the smooth underlying distribution. This is a consequence of the typical behavior we see in disturbed bands and shown, as an example, in Figure 66 when the measured detection efficiency does not closely follow the Weibull fitting function, see Eq. 5 , in the interval around the $95 \%$ level, the resulting upper limit can be significantly larger with respect to the value expected for a quiet band. We have verified that such fluctuations could be significantly reduced by increasing the number of candidates selected at the ranking level: for instance going from 4 to 8 would yield much smoother results (at the price of doubling the number of follow-ups to be done). There are some highly disturbed

| Label | Frequency <br> Hz | Spindown <br> $\mathrm{nHz} / \mathrm{s}$ | RA $_{\text {J2000 }}$ <br> degrees | DEC $_{\text {J2000 }}$ <br> degrees |
| :--- | ---: | ---: | ---: | :---: |
| ip0 | 265.575533 | $-4.15 \times 10^{-3}$ | 71.55193 | -56.21749 |
| ip1 | 848.969641 | $-3.00 \times 10^{-1}$ | 37.39385 | -29.45246 |
| ip2 | 575.163521 | $-1.37 \times 10^{-4}$ | 215.25617 | 3.44399 |
| ip3 | 108.857159 | $-1.46 \times 10^{-8}$ | 178.37257 | -33.4366 |
| ip4 | 1393.540559 | $-2.54 \times 10^{-1}$ | 279.98768 | -12.4666 |
| ip5 | 52.808324 | $-4.03 \times 10^{-9}$ | 302.62664 | -83.83914 |
| ip6 | 146.169370 | $-6.73 \times 10^{0}$ | 358.75095 | -65.42262 |
| ip7 | 1220.555270 | $-1.12 \times 10^{0}$ | 223.42562 | -20.45063 |
| ip8 | 191.031272 | $-8.65 \times 10^{0}$ | 351.38958 | -33.41852 |
| ip9 | 763.847316 | $-1.45 \times 10^{-8}$ | 198.88558 | 75.68959 |
| ip10 | 26.341917 | $-8.50 \times 10^{-2}$ | 221.55565 | 42.87730 |
| ip11 | 31.424758 | $-5.07 \times 10^{-4}$ | 285.09733 | -58.27209 |
| ip12 | 38.477939 | $-6.25 \times 10^{0}$ | 331.85267 | -16.97288 |
| ip13 | 12.428001 | $-1.00 \times 10^{-2}$ | 14.32394 | -14.32394 |
| ip14 | 1991.092401 | $-1.00 \times 10^{-3}$ | 300.80284 | -14.32394 |

TABLE IV. Parameters of the hardware-injected simulated continuous-wave signals during the O1 data run (epoch GPS 1130529362 ). Because the interferometer configurations were largely frozen in a preliminary state after the first discovery of gravitational waves from a binary black hole merger, the hardware injections were not applied consistently. There were no injections in the H1 interferometer initially, and the initial injections in the L1 interferometer used an actuation method with significant inaccuracies at high frequencies.


FIG. 16. Range of the PowerFlux search for neutron stars spinning down solely due to gravitational radiation. This is a superposition of two contour plots. The grey and red solid lines are contours of the maximum distance at which a neutron star could be detected as a function of gravitational-wave frequency $f$ and its derivative $\dot{f}$. The dashed lines are contours of the corresponding ellipticity $\epsilon(f, \dot{f})$. The fine dotted line marks the maximum spindown searched. Together these quantities tell us the maximum range of the search in terms of various populations (see text for details) (color online). The other three search pipelines have similar ranges for circularly polarized sources.
bands, especially below 40 Hz , for which we are unable to compute the upper limit because the detection efficiency never reaches the $95 \%$ level.

As a further test of the capabilities of the pipeline to recover signals, in addition to those shown in Sec. IV B 1, we report in Tab. $V$ parameters of the recovered hardware injections, together with the error with respect to the injected signals. In general we find a good agreement (with the exception of ip5 and ip12, which are missed).

## D. SkyHough search results

In this section we report the main results of the O1 allsky search between 50 and 500 Hz using the SkyHough pipeline, as described in section IV C. In total, 194 0.1Hz bands contained coincidence candidates, and therefore 194 coincidence clusters were identified and further investigated. The majority of these outliers corresponded to known spectral lines, severe spectral disturbances or hardware injected signals.

This initial list was reduced to 59 after applying the cluster population veto and to 26 after the multiinterferometer consistency veto. A detailed list of these remaining outliers is shown in Table XII. The multiinterferometer significance consistency veto alone was able to reduce the initial list of 194 candidates to 33 .

Of these 26 outliers, 5 corresponded to hardware injected pulsars and 20 to known line artifacts contaminating either H1 or L1 data. The only unexplained outlier around 452.89989 Hz is due to an unknown large spectral disturbance in the H1 detector. Table VI in Appendix C provides details on these outliers.

Therefore this search did not find any evidence of a


FIG. 17. Upper limits for the FrequencyHough pipeline, in the range between 20 Hz and 475 Hz .

| Label | CR | Frequency $[\mathrm{Hz}]$ | Spin-down $[\mathrm{nHz} / \mathrm{s}]$ | $\alpha[\mathrm{deg}]$ | $\delta[\mathrm{deg}]$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| ip10 | 37.9 | $26.34211(0.00019)$ | $-0.0671(0.0179)$ | $219.6584(-1.896)$ | $43.6464(0.769)$ |
| ip11 | 118.5 | $31.42512(0.00027)$ | $-0.0742(-0.0736)$ | $274.4572(-10.640)$ | $-49.2362(9.033)$ |
| ip3 | 87.8 | $108.85705(-0.00011)$ | $0.01645(0.0164)$ | $177.5770(-0.795)$ | $-34.1960(-0.759)$ |
| ip6 | 42.2 | $146.16382(-0.00045)$ | $-6.7099(0.0201)$ | $358.6904(-0.061)$ | $-65.2405(0.182)$ |
| ip8 | 138.6 | $191.02390(-0.00013)$ | $-8.7161(-0.0661)$ | $351.2037(-0.186)$ | $-35.0975(-1.679)$ |
| ip0 | 180.7 | $265.57572(0.00019)$ | $-0.0483(-0.0441)$ | $73.0276(1.476)$ | $-57.0156(-0.798)$ |

TABLE V. Hardware injection recovery with the FrequencyHough pipeline. The reported values have been obtained at the end of the full analysis, including the follow-up. The values in parentheses are the absolute errors, that is the difference with respect to the injection parameters. The reference time is MJD=57328.59684. Two hardware injections are not accurately found (and not reported in the table): ip5 and ip12. In both cases the analysis detected "children" of the injected signal, with parameters significantly different from those of the injection. Injection ip11 has been discarded in the last stage of the follow-up because it did not pass the CR consistency veto among single detectors, although its parameters are recovered with good accuracy.

| Label $s_{\text {mean }}$ | Frequency <br> $[\mathrm{Hz}]$ | Spin-down <br> $[\mathrm{nHz} / \mathrm{s}]$ | $\alpha$ <br> $[\mathrm{deg}]$ | $\delta$ <br> $[\mathrm{deg}]$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| ip5 | 24.22 | $52.8084(0.0001)$ | $-0.0175(0.0175)$ | 294.2376 | $(8.3890)$ |$-83.1460(0.6932)$

TABLE VI. SkyHough hardware injection cluster information. The table provides the frequency, spin-down and sky location of the cluster center related to each of the hardware injections found by the SkyHough search. In parentheses the absolute errors with respect to the injected values are shown. Frequencies are converted to epoch GPS 1125972653.
continuous gravitational wave signal. Upper limits have been computed in each $0.1-\mathrm{Hz}$ band, except for the 194 bands in which outliers were found.

## E. Time-Domain $\mathcal{F}$-statistic search results

In the bandwidth searched $[10,475] \mathrm{Hz}, 19210.25-\mathrm{Hz}$ long bands were defined (see Eq. 13). As a result of vetoing candidates around the known interference lines, a certain fraction of the bandwidth was not analyzed. In Figure 19 we show the fraction of the bandwidth vetoed for each band. As a result $22 \%$ of the $[10,475] \mathrm{Hz}$ band was vetoed, overall.

Of 1921 bands analyzed, 38 bands were completely vetoed because of line artifacts. As a result of the coherent search in 15368 data segments, we obtained around $6.2 \times 10^{11}$ candidates. These candidates were subject to a search for initial coincidences in a second stage of the Time-Domain $\mathcal{F}$-statistic analysis. The search for coincidences was performed in all the bands except for the above-mentioned 38 that were completely vetoed. Also, in addition to the 38 bands vetoed because of line artifacts, there were 13 highly disturbed bands for which no coincidence results were obtained because there were too many candidates for the current coincidence program to handle properly. In the coincidence analysis, for each band, the coincidences among the candidates were searched in eight 6 -day long time frames. In Figure 20 the results of the coincidence search are presented. The top panel shows the maximum coincidence multiplicity for each of the bands analyzed. The maximum multiplicity is an integer that varies from 3 to 8 because we require coincidence multiplicity of at least 3 , and 8 is the number of time frames analyzed.

The bottom panel of Fig. 20 shows the results for the false alarm probability of coincidence for the coincidence with the maximum multiplicity. This false alarm probability is calculated using the formula from the Appendix of [19].

For further analysis 49 coincidences with the lowest false alarm probability were selected. The parameters of these coincidences are listed in Table XIII in Appendix D. they are the outliers of the search. The parameters of a given coincidence are calculated as the mean values of the parameters of the candidates that enter a given coincidence. Among these 49 outliers, 11 are identified with the hardware injections. Table VII presents the estimated parameters obtained for these hardware injections, along with the absolute errors of the reconstructed parameters (the differences with respect to the injected parameters). The remaining 38 outliers include 6 associated with the 0.25 Hz comb, 15 seen in only one interferometer, 4 in only the first half of the run, 1 transient disturbance, 8 corresponding to PowerFlux outliers already excluded, and 2 (numbers 10 and 11) requiring further, deep followup (although inconsistent structures seen in run-averaged H1 and L1 spectra in that band already cast doubt on an
astrophysical origin). The deep follow-up used the same method [31, 32] as for persistent outliers in the other search pipelines. Again, no credible signals were found.

## VI. CONCLUSIONS

We have performed the most sensitive all-sky searches to date for continuous gravitational waves in the range $20-475 \mathrm{~Hz}$, using four independent search programs that apply a variety of algorithmic approaches with different parameter choices and different approaches to handling instrumental contaminations. The overall improvements in strain sensitivity come primarily from the improved noise floors of the Advanced LIGO interferometers over previous LIGO and Virgo interferometers, with reductions in upper limits of about a factor of 3 at frequencies above 100 Hz and larger reductions at lower frequencies. We explored both positive and negative spindowns and found no credible gravitational wave signals, allowing upper limits to be placed on possible source signal amplitudes. Fig. 21 shows a summary of the strain amplitude upper limits obtained for the four pipelines. Three of the pipelines (FrequencyHough, SkyHough, Time-Domain $\mathcal{F}$-statistic) present population-averaged limits over the full sky and source polarization, while one pipeline (PowerFlux) presents strict all-sky limits for circularpolarization and linear-polarization sources.

At the highest frequencies we are sensitive to neutron stars with an equatorial ellipticity as small as $8 \times 10^{-7}$ and as far away as 1 kpc for favorable spin orientations. The maximum ellipticity a neutron star can theoretically support is at least $1 \times 10^{-5}$ according to [50, 51]. Our results exclude such maximally deformed pulsars above 200 Hz pulsar rotation frequency $(400 \mathrm{~Hz}$ gravitational frequency) within 1 kpc . Outliers from initial stages of each search method were followed up systematically, but no candidates from any search survived scrutiny.

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FIG. 18. Time-Domain $\mathcal{F}$-statistic pipeline O1 upper limits. Black dots are the $95 \%$ confidence upper limits for each frequency, the red line denotes the H1 and L1 detectors' average noise curve rescaled by the factor $27.5 / \sqrt{T_{0}}$, where $T_{0}=516984 \mathrm{~s}$ is the observational time of the 6 -day time series segment (color online).

| Label FA | Frequency $[\mathrm{Hz}]$ | Spin-down $[\mathrm{nHz} / \mathrm{s}]$ | $\alpha[\mathrm{deg}]$ | $\delta[\mathrm{deg}]$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| ip0 | 70 | $265.57565(-0.00012)$ | $0.2582(-0.2602)$ | $68.6196(2.932)$ | $-53.7294(-2.488)$ |
| ip3 | 19 | $108.85713(-0.00003)$ | $0.0158(0.0158)$ | $172.0773(6.295)$ | $-30.6495(-2.787)$ |
| ip5 | 30 | $52.8085(-0.00015)$ | $-0.2168(0.2168)$ | $273.6538(28.972)$ | $-63.6095(-20.230)$ |
| ip6 | 34 | $146.16861(-0.00064)$ | $-6.8469(0.1169)$ | $350.4083(8.343)$ | $-64.2301(-1.192)$ |
| ip8 | 23 | $191.02942(0.00004)$ | $-8.2475(-0.4024)$ | $340.2146(11.175)$ | $8.6891(-42.108)$ |
| ip10 | 55 | $26.34206(-0.00016)$ | $-0.0763(0.0087)$ | $226.9401(-5.384)$ | $41.1968(1.680)$ |
| ip11 | 89 | $31.42490(-0.00014)$ | $-0.0798(-0.803)$ | $301.7315(-16.634)$ | $-53.2623(5.010)$ |

TABLE VII. Hardware injection recovery with the Time-Domain $\mathcal{F}$-statistic pipeline. The values in parentheses are the absolute errors, that is, the difference with respect to the injection parameters. Frequencies are converted to epoch GPS 1130737464.
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FIG. 19. Fraction of the bandwidth vetoed for each band searched by the Time-Domain $\mathcal{F}$-statistic pipeline.


FIG. 20. Time-Domain $\mathcal{F}$-statistic pipeline coincidences results as a function of the band frequency. Top panel: maximum coincidence multiplicity. Bottom panel: false alarm probability for the coincidence with the maximum multiplicity.

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## Appendix A: PowerFlux outlier tables

PowerFlux outliers are separated into three categories. Of the most interest are outliers in table VIII spanning 2 or more segments that are outside a known comb of 0.25 Hz lines. Outliers spanning only one segment are presented in table IX. Finally the table X lists outliers near 0.25 Hz comb.

## Appendix B: FrequencyHough outlier tables

In this section we describe in some detail the final outliers found in the FrequencyHough search and the analyses that have been carried on them. Tab. XI contains the list of the outliers and their main characteristic, including a brief comment. Each of these outliers has been manually examined by looking at the details of the follow-up products, including the peakmaps and the Hough maps, and comparing single detector and joint results. For all of these outliers a gravitational wave origin can be excluded. For outliers 2-5 and 10 in Table XI the presence of instrumental artifacts (of unknown origin) is clear. Outliers $1,6,8,11$ and 13 are not consistent between the two detectors. In particular, n. 8 and 11 are attributed to transient disturbance in the Hanford detector. Outlier 9 is consistent between detectors, but not highly significant in the two detectors. Finally, outliers 7, 12 and 14 were potentially more interesting: they are consistent among the two detectors, very significant also in the single-interferometer analysis, and the corresponding Hough maps look reasonable. As an example in Fig. 22 we plot the corrected peakmap projections for outlier 7, and in Fig. 23 the outlier joint Hough map. For these outliers we have carried out a deeper follow-up using the method described in [31, 32], with a coherence time of 210 hours. In all cases the follow-up failed to yield a credible signal. Hence none of the above outliers shows evidence of a true gravitational wave signal

## Appendix C: SkyHough outlier tables

Table XII presents the parameters of the final 26 outliers from the SkyHough search pipeline, along with comments on their likely causes. None is a credible gravitational wave signal.

## Appendix D: Time-Domain $\mathcal{F}$-statistic outlier tables

Table XIII presents the parameters of the final 49 outliers from the Time-Domain $\mathcal{F}$-statistic pipeline, along with comments on their likely causes. None is a credible gravitational wave signal.


FIG. 21. (Color online) Upper limit comparison for the four search pipelines used in this analysis. The curves represent the source strain amplitude $h_{0}$ at which $95 \%$ of simulated signals would be detected. Three of the pipelines (FrequencyHough, SkyHough, Time-Domain $\mathcal{F}$-statistic) present population-averaged limits over the full sky and source polarization, while one pipeline (PowerFlux) presents strict all-sky limits for circular-polarization (most favorable orientation - black) and linearpolarization (least favorable orientation - cyan) sources. Converting the PowerFlux upper limits to validated populationaveraged upper limits would require extensive, band-dependent Monte Carlo simulations, but previous studies suggest that such limits would lie in a region similar to that of the other pipelines. In addition, the population-averaged upper limits from the most recent Einstein@Home search are shown for comparison 32. The Einstein@Home search explored the low frequencies, and a narrower spindown range using a much longer coherence length (210 hours).

| Idx | SNR | Segment | $\begin{gathered} \text { Frequency } \\ \mathrm{Hz} \end{gathered}$ | $\begin{gathered} \text { Spindown } \\ \mathrm{nHz} / \mathrm{s} \\ \hline \end{gathered}$ | $\begin{gathered} \hline \text { RA }_{\text {J2000 }} \\ \text { degrees } \\ \hline \end{gathered}$ | $\mathrm{DEC}_{\mathrm{J} 2000}$ degrees | Description |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 10532 | [0, 2] | 256.00854 | -1.475 | 255.225 | -85.537 | Extremely strong bin-centered line at 256.0 Hz |
| 33 | 352 | [1, 2] | 52.80829 | 0.000 | 301.148 | -84.274 | Hardware injection ip5 |
| 36 | 269 | [0, 2] | 191.03127 | -8.663 | 351.292 | -33.643 | Hardware injection ip8 |
| 37 | 236 | [1, 2] | 265.57551 | -0.013 | 71.719 | -56.276 | Hardware injection ip0 |
| 39 | 227 | $[0,1]$ | 21.41061 | -0.500 | 230.715 | $-1.630$ | Sharp line in L1 near $21.41 \mathrm{~Hz}, \mathrm{H} 1$ and L1 SNR inconsistent |
| 46 | 172 | [1, 2] | 146.16942 | $-6.775$ | 356.992 | -65.953 | Hardware injection ip6 |
| 47 | 170 | [0, 1] | 31.11704 | $-7.362$ | 56.406 | -22.568 | Coincident combs with different morphology between H1 and L1 |
| 52 | 145 | [1, 2] | 108.85708 | 0.037 | 176.861 | -34.170 | Hardware injection ip3 |
| 56 | 110 | $[0,1]$ | 59.60507 | 0.113 | 283.407 | 68.377 | Coincident lines in spectrum, signal nearly stationary in detector frame |
| 70 | 63 | $[1,2]$ | 99.96961 | 1.775 | 99.689 | 35.244 | Coincident regions between H1 and L1 |
| 72 | 52 | [1, 2] | 30.63391 | -6.688 | 357.777 | -40.140 | Both H1 and L1 spectra are contaminated |
| 74 | 48 | [1, 2] | 412.00362 | -0.588 | 84.695 | $-71.077$ | Sharp bin-centered line in L1 at 412.0 Hz |
| 78 | 39 | [0, 1] | 93.75912 | 0.062 | 279.035 | $-13.320$ | Sharp and coincident lines in H1 and L1, SNR inconsistent |
| 85 | 33 | [0, 1] | 299.42508 | 1.175 | 317.303 | 46.331 | All SNR comes from large artifact in H1 |
| 95 | 23 | [0, 2] | 90.74396 | 0.250 | 86.019 | -18.203 | Coincident bin-centered lines at $90.75 \mathrm{~Hz}, 0.25 \mathrm{~Hz}$ comb |
| 98 | 19 | [0, 2] | 33.59221 | 0.300 | 359.165 | $-18.874$ | Both H1 and L1 spectra are disturbed, H1 does not see anything |
| 99 | 19 | [1, 2] | 306.01509 | -2.275 | 130.248 | 33.827 | Large artifact in L1, H1 does not see anything |
| 100 | 19 | [0, 2] | 299.39436 | -0.287 | 116.867 | 73.521 | Large artifact in H1, L1 does not see anything |
| 102 | 17 | [0, 2] | 307.31880 | -6.612 | 181.054 | -25.115 | Large artifact in L1, H1 does not see anything |
| 109 | 16 | $[0,1]$ | 452.88717 | 0.238 | 82.204 | -67.295 | Large artifact in H1 |
| 122 | 14 | [1, 2] | 452.86305 | -2.350 | 198.764 | 49.143 | Large artifact in H1 |
| 128 | 13 | [1, 2] | 29.63552 | 0.312 | 107.619 | 1.373 | Coincident disturbances with different morphologies in H1 and L1 |
| 134 | 13 | [1, 2] | 265.75911 | -2.112 | 67.964 | -28.799 | Not confirmed by Einstein@Home followup |
| 138 | 13 | $[0,1]$ | 178.60606 | -3.275 | 194.163 | 51.285 | Sharp line in L1 at 178.7 Hz is outside signal range |
| 154 | 12 | [1, 2] | 404.79214 | -6.675 | 136.431 | 38.381 | Not confirmed by Einstein@Home followup |

TABLE VIII. Outliers that passed PowerFlux detection pipeline spanning more than one segment and excluding those near a $0.25-\mathrm{Hz}$ comb. Only the highest-SNR outlier is shown for each $0.1-\mathrm{Hz}$ frequency region. Outliers marked with "line" had strong narrowband disturbances identified near the outlier location. The "Segment" column reports the set of contiguous segments of the data that produced the outlier, as described in Section V. Frequencies are converted to epoch GPS 1130529362.

| Idx | SNR | Segment | $\begin{gathered} \text { Frequency } \\ \mathrm{Hz} \end{gathered}$ | Spindown nHz/s | $\begin{gathered} \mathrm{RA}_{\mathrm{J} 2000} \\ \text { degrees } \end{gathered}$ | DEC $_{J 2000}$ degrees | Description |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 5470 | [1, 1] | 35.70737 | -0.287 | 71.099 | -89.596 | Broadly coincident region between 35.7 and 35.71 |
| 22 | 933 | [2, 2] | 35.76455 | -0.700 | 241.377 | $-7.873$ | Broadly coincident region |
| 31 | 417 | [1, 1] | 59.51547 | -2.112 | 282.450 | 16.555 | Coincident regions |
| 40 | 223 | [1, 1] | 83.31080 | -2.000 | 184.935 | -16.484 | Coincident regions between H1 and L1 |
| 41 | 197 | [0, 0] | 100.00749 | 0.650 | 319.773 | -59.068 | Coincident regions between H1 and L1 |
| 43 | 185 | [0, 0] | 113.68611 | 1.062 | 26.888 | -57.341 | Strong line in H1, H1 and L1 SNR inconsistent |
| 45 | 177 | [2, 2] | 31.42488 | -0.062 | 278.446 | -49.515 | Coincident regions between H 1 and L1, is this really an injection |
| 48 | 163 | [2, 2] | 46.95114 | -0.350 | 132.597 | -88.847 | Coincident sharp lines at 46.95 |
| 49 | 152 | [2, 2] | 38.47802 | -6.312 | 326.542 | -17.113 | Hardware injection ip12 |
| 57 | 108 | [2, 2] | 440.50273 | 1.762 | 65.270 | -37.191 | Sharp line in L1 at 440.5 |
| 62 | 86 | [0, 0] | 40.87517 | 0.375 | 236.742 | 79.741 | Elevated and disturbed spectrum, uneven sensitivity during run |
| 66 | 70 | $[1,1]$ | 31.76233 | 0.613 | 64.921 | -9.503 | Coincident lines in H1 and L1 |
| 77 | 39 | [1, 1] | 39.76505 | -0.250 | 298.570 | 42.651 | Sharp and coincident lines in H1 and L1 |
| 82 | 37 | [2, 2] | 78.50513 | -0.688 | 299.793 | 45.680 | Sharp and coincident lines at $78.5 \mathrm{~Hz}, 0.25 \mathrm{~Hz}$ comb |
| 83 | 34 | [2, 2] | 128.49647 | 0.962 | 323.700 | 86.937 | Outlier favors region next to the line at 128.5 Hz |
| 87 | 32 | [1, 1] | 32.60162 | -0.912 | 221.578 | 10.228 | All SNR comes from disturbance in L1 |
| 89 | 29 | [2, 2] | 127.50310 | -0.900 | 135.660 | -85.458 | Coincident bin-centered lines at 127.5 Hz in both ifos |
| 90 | 28 | [1, 1] | 47.68505 | -4.125 | 80.941 | -75.614 | H1 and L1 disagree on location, common overlapping artifact |
| 92 | 24 | [0, 0] | 246.30806 | -0.800 | 257.315 | -88.956 | Coincident bin-centered lines at 246.3 Hz |
| 96 | 22 | [0, 0] | 453.38509 | -7.400 | 213.641 | 21.911 | Large artifact in H1, L1 does not see anything |
| 97 | 22 | [0, 0] | 70.92119 | 0.275 | 136.639 | -68.924 | Coincident artifacts in H1 and L1 |
| 101 | 17 | [0, 0] | 306.00102 | -6.513 | 106.860 | -14.138 | Small disturbance in L1 |
| 104 | 17 | [2, 2] | 26.36415 | -9.013 | 62.782 | -13.429 | Coincident combs, large artifact with different morphology in H1 and L1 |
| 105 | 16 | [1, 1] | 43.68056 | 0.087 | 114.317 | -3.107 | Large artifact in L1 |
| 106 | 16 | [0, 0] | 327.59196 | -8.162 | 23.524 | -50.419 |  |
| 107 | 16 | [1, 1] | 31.61544 | 0.238 | 17.372 | -10.319 | Different disturbances in H1 and L1 spectrum |
| 108 | 16 | [0, 0] | 308.99815 | -3.925 | 289.216 | 47.738 |  |
| 110 | 15 | [1, 1] | 337.31874 | -0.675 | 244.827 | 41.178 |  |
| 111 | 15 | [0, 0] | 350.25984 | -8.188 | 313.477 | -34.804 |  |
| 112 | 15 | [0, 0] | 345.08507 | 0.900 | 136.135 | 40.606 |  |
| 113 | 15 | [0, 0] | 453.35293 | -5.725 | 143.703 | 64.705 | Appears to be associated with artifact at 453.40 Hz |
| 114 | 14 | [0, 0] | 254.15359 | -9.938 | 204.993 | 43.892 | Weak sharp line in L1 at 241.1 Hz |
| 115 | 14 | [0, 0] | 436.09611 | -6.750 | 346.514 | -36.245 |  |
| 116 | 14 | [0, 0] | 310.92629 | -3.975 | 359.968 | 14.226 |  |
| 117 | 14 | $[1,1]$ | 162.18514 | -1.587 | 101.520 | -3.877 |  |
| 118 | 14 | [2, 2] | 454.18958 | -4.138 | 254.665 | 0.668 | Sharp line in L1 at 454 Hz is outside signal range |
| 119 | 14 | [1, 1] | 225.64096 | -2.725 | 234.719 | 31.199 | Large artifact in H1 |
| 120 | 14 | [0, 0] | 394.54298 | -2.238 | 147.069 | 51.380 |  |
| 121 | 14 | $[1,1]$ | 270.50488 | 1.025 | 192.977 | 26.380 | Sharp line in L1 at 270.5 is outside signal range |
| 123 | 14 | [2, 2] | 213.68406 | 0.413 | 203.168 | 36.792 |  |
| 124 | 14 | [1, 1] | 293.36763 | -0.725 | 291.910 | -39.555 |  |
| 125 | 13 | [1, 1] | 336.94860 | -1.212 | 29.971 | -40.200 |  |
| 126 | 13 | $[1,1]$ | 318.76465 | -7.375 | 203.369 | 39.161 | Sharp line in L1 at 318.80 Hz is outside signal range |
| 127 | 13 | [1, 1] | 97.00786 | -4.338 | 152.289 | 42.607 | Sharp line in L1 at 97.1 Hz is outside signal range |
| 129 | 13 | [2, 2] | 446.76910 | -5.237 | 275.842 | 27.684 |  |
| 130 | 13 | [2, 2] | 415.31493 | -0.625 | 246.343 | 35.521 | Sharp line in L1 at 415.4 Hz is outside signal range |
| 131 | 13 | [1, 1] | 289.16717 | -4.812 | 289.555 | 56.661 | Sharp line in L 1 at 289.3 Hz is outside signal range |
| 132 | 13 | [2, 2] | 435.04082 | 1.175 | 61.748 | -49.375 |  |
| 133 | 13 | [0, 0] | 353.38444 | $-7.325$ | 267.522 | 65.417 |  |
| 135 | 13 | [0, 0] | 247.50050 | -5.975 | 60.313 | -25.256 | Sharp line in L1 at 247.3 is outside signal range |
| 136 | 13 | [0, 0] | 463.10329 | -1.700 | 30.527 | -20.284 | Sharp line in L1 at 463.2 Hz is outside signal range |
| 137 | 13 | $[1,1]$ | 380.57045 | -9.338 | 244.202 | 45.262 | Sharp line in L1 at 480.6 Hz is outside signal range |
| 139 | 13 | [2, 2] | 443.65961 | -1.988 | 82.034 | -43.630 |  |
| 140 | 13 | [1, 1] | 442.16364 | -6.525 | 80.319 | 31.835 |  |
| 141 | 13 | [2, 2] | 437.40225 | -9.825 | 139.879 | -37.221 | Lines in H1 and L1 outside signal range |
| 142 | 13 | $[1,1]$ | 474.28332 | -8.562 | 354.078 | 39.661 | Sharp line in L1 at 474.3 |
| 143 | 13 | [0, 0] | 232.64393 | -7.500 | 244.442 | 30.182 | Sharp line in L1 at 232.8 |
| 144 | 13 | [2, 2] | 455.60513 | -9.125 | 264.100 | 12.723 | Identical slope in H1 and L1 spectrum |
| 145 | 13 | [2, 2] | 321.96324 | -5.425 | 88.612 | -18.667 | Disturbed H1 spectrum |
| 146 | 13 | [0, 0] | 377.36117 | -3.900 | 162.703 | 19.347 |  |
| 147 | 13 | [1, 1] | 463.81555 | -2.762 | 92.427 | -21.270 | Sharp line in L1 at 463.7 is outside signal range |
| 148 | 12 | [2, 2] | 369.43296 | 1.113 | 318.118 | 43.385 | Sharp line in L1 at 369.5 is outside signal range |
| 149 | 12 | [0, 0] | 348.24255 | -2.862 | 249.590 | 53.903 | Sharp line in L1 at 348.2 is outside signal range |
| 150 | 12 | $[1,1]$ | 293.17864 | -1.713 | 1.204 | 9.380 |  |
| 151 | 12 | $[1,1]$ | 371.37093 | -9.562 | 17.812 | -38.934 |  |
| 152 | 12 | [2, 2] | 418.80178 | -9.588 | 180.042 | -37.122 |  |
| 153 | 12 | [0, 0] | 56.38793 | 0.812 | 11.265 | -26.818 | Rather large disturbance in L1 outside signal range |
| 155 | 12 | [1, 1] | 389.58663 | 0.375 | 190.109 | 39.234 |  |
| 156 | 12 | [1, 1] | 381.17708 | -8.162 | 327.725 | -27.100 | Sharp line in L1 at 381.1 is outside signal range |
| 157 | 12 | [1, 1] | 471.92300 | 0.800 | 351.848 | -37.756 | Sharp line in H1 at 472 Hz , sharp line in L1 471.9 Hz |
| 158 | 12 | [0, 0] | 231.41586 | -6.038 | 151.842 | 51.699 |  |
| 159 | 12 | [1, 1] | 384.21151 | -5.938 | 205.820 | 36.442 | Sharp line in H 1 at 384 Hz is far outside signal range |
| 160 | 12 | [2, 2] | 359.81255 | -0.875 | 278.065 | 26.246 | Outlier favors sidelobes of 60 Hz harmonic |
| 161 | 12 | [0, 0] | 302.90153 | 0.150 | 323.285 | -57.949 |  |

TABLE IX. Outliers that passed PowerFlux detection pipeline spanning only one segment, excluding those near $0.25-\mathrm{Hz}$ comb. Only the highest-SNR outlier is shown for each $0.1-\mathrm{Hz}$ frequency region. Outliers marked with "line" had strong narrowband disturbances identified near the outlier location. Segment column reports the set of contiguous segments of the data that produced the outlier, as described in $V$ Frequencies are converted to epoch GPS 1130529362.

| Idx | SNR | Segment | $\begin{gathered} \hline \text { Frequency } \\ \mathrm{Hz} \\ \hline \end{gathered}$ | Spindown $\mathrm{nHz} / \mathrm{s}$ | $\begin{gathered} \mathrm{RA}_{\mathrm{J} 2000} \\ \text { degrees } \end{gathered}$ | $\begin{gathered} \hline \text { DEC }_{\text {J2000 }} \\ \text { degrees } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 5603 | [1, 2] | 21.50025 | -0.150 | 151.422 | -79.107 |
| 4 | 4996 | [1, 2] | 34.49925 | 0.350 | 21.714 | 77.506 |
| 5 | 4938 | [0, 2] | 25.00029 | -0.413 | 234.953 | 13.114 |
| 7 | 4207 | [0, 2] | 29.50008 | -0.150 | 131.116 | -74.570 |
| 10 | 2921 | [1, 2] | 20.49974 | 0.113 | 309.323 | 79.014 |
| 11 | 2721 | [0, 2] | 33.24851 | -0.050 | 196.925 | 82.946 |
| 15 | 1593 | [0, 2] | 47.49882 | 0.463 | 23.877 | 80.095 |
| 17 | 1493 | [1, 2] | 46.49823 | 0.725 | 55.515 | 60.238 |
| 18 | 1238 | [0, 1] | 23.24905 | 0.263 | 62.224 | 5.482 |
| 19 | 1161 | [0, 2] | 31.25038 | -0.137 | 156.015 | -78.649 |
| 23 | 914 | [0, 2] | 54.50016 | 0.275 | 311.453 | 70.504 |
| 25 | 837 | [0, 2] | 22.24910 | -0.413 | 201.320 | 17.588 |
| 27 | 615 | [0, 2] | 58.50283 | -0.575 | 293.833 | -81.976 |
| 28 | 587 | [0, 2] | 57.49720 | 1.012 | 65.281 | 51.741 |
| 29 | 551 | [0, 2] | 41.50357 | -0.450 | 314.469 | -57.748 |
| 30 | 421 | [0, 2] | 43.24808 | -0.062 | 221.374 | 82.111 |
| 35 | 305 | [0, 1] | 48.24916 | -0.200 | 246.369 | 59.628 |
| 38 | 229 | [0,2] | 20.24852 | 0.025 | 94.536 | -6.808 |
| 44 | 179 | [0, 1] | 27.24799 | -1.475 | 248.015 | -15.916 |
| 50 | 151 | [0, 2] | 50.24710 | -0.037 | 134.356 | 86.279 |
| 53 | 141 | [1, 2] | 42.99932 | 0.325 | 341.196 | 79.984 |
| 54 | 140 | [1, 2] | 34.24893 | 0.450 | 43.246 | 68.520 |
| 59 | 106 | [0, 1] | 66.75438 | 0.175 | 29.149 | 89.424 |
| 60 | 98 | [0, 2] | 38.99998 | -0.025 | 94.142 | -67.898 |
| 63 | 85 | [0, 1] | 85.50355 | -0.537 | 285.886 | -82.302 |
| 64 | 79 | [1, 2] | 40.00031 | -0.175 | 115.403 | -76.647 |
| 65 | 76 | [0, 2] | 45.00071 | 0.062 | 17.453 | -83.230 |
| 67 | 68 | [1, 2] | 39.25073 | -0.525 | 215.636 | -65.846 |
| 68 | 66 | [0,2] | 98.49708 | 0.750 | 330.835 | 87.908 |
| 76 | 44 | [1, 2] | 21.24994 | -0.037 | 255.942 | 63.243 |
| 86 | 32 | [0, 2] | 88.75324 | -0.062 | 212.757 | -88.557 |
| 91 | 25 | [0, 2] | 89.75337 | 0.775 | 317.050 | 51.127 |
| 93 | 24 | [0, 2] | 91.75467 | -0.338 | 260.215 | 23.279 |
| 103 | 17 | [0, 2] | 97.75447 | -1.075 | 245.495 | -8.107 |
| 6 | 4508 | [2, 2] | 23.50090 | -0.250 | 240.850 | -80.885 |
| 8 | 3346 | [2, 2] | 42.49877 | 0.400 | 30.333 | 83.056 |
| 9 | 3071 | [1, 1] | 28.49919 | 0.250 | 35.734 | 80.126 |
| 12 | 2269 | [2, 2] | 36.50033 | 0.200 | 329.266 | 68.973 |
| 13 | 2218 | [0, 0] | 30.50049 | 0.062 | 66.712 | -70.484 |
| 14 | 1864 | [0, 0] | 33.49977 | 0.025 | 272.862 | 72.497 |
| 16 | 1581 | [1, 1] | 24.50010 | 0.163 | 327.225 | 69.131 |
| 20 | 1155 | [1, 1] | 31.49812 | -0.150 | 183.141 | 56.041 |
| 21 | 1112 | [1, 1] | 39.50029 | -0.400 | 182.468 | -69.888 |
| 24 | 881 | [0, 0] | 37.50214 | 0.050 | 308.365 | -78.677 |
| 26 | 652 | [0, 0] | 48.50039 | 0.087 | 283.523 | 66.911 |
| 32 | 414 | [0, 0] | 25.24979 | 0.312 | 48.291 | -15.967 |
| 34 | 339 | [0, 0] | 25.49812 | -0.200 | 163.735 | 61.435 |
| 42 | 194 | [2, 2] | 71.50111 | -0.438 | 261.002 | 49.485 |
| 51 | 148 | [2, 2] | 26.25072 | -0.275 | 212.451 | -78.398 |
| 55 | 122 | [0, 0] | 60.50055 | 0.087 | 281.309 | 63.866 |
| 58 | 107 | [1, 1] | 31.99943 | 0.250 | 6.435 | 78.791 |
| 61 | 97 | [1, 1] | 30.00010 | -0.200 | 147.604 | -74.370 |
| 69 | 65 | [0, 0] | 30.99823 | 0.087 | 76.765 | 69.482 |
| 71 | 57 | [2, 2] | 84.99812 | 0.525 | 292.900 | 84.017 |
| 73 | 52 | [1, 1] | 37.25095 | -0.338 | 218.785 | -80.271 |
| 75 | 44 | [2, 2] | 57.00140 | -0.463 | 175.217 | -84.532 |
| 79 | 39 | [2, 2] | 46.25171 | -0.713 | 240.550 | -62.392 |
| 80 | 38 | [2, 2] | 44.25014 | -0.250 | 132.213 | -77.498 |
| 81 | 37 | [2, 2] | 38.00200 | -0.762 | 250.147 | -18.662 |
| 84 | 33 | [1, 1] | 36.25184 | -0.400 | 270.188 | -69.467 |
| 88 | 31 | [1, 1] | 50.00082 | -0.325 | 148.358 | -81.767 |
| 94 | 23 | [2, 2] | 41.24653 | -0.100 | 150.901 | -22.875 |

TABLE X. PowerFlux outliers below 100 Hz found within 5 mHz of 0.25 Hz comb. Only the highest-SNR outlier is shown for each $0.1-\mathrm{Hz}$ frequency region. Segment column reports the set of contiguous segments of the data that produced the outlier, as described in V Frequencies are converted to epoch GPS 1130529362.

| Idx Frequency $[\mathrm{Hz}]$ |  |  |  |  |  | Spin-down $[\mathrm{Hz} / \mathrm{s}]$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\alpha[\mathrm{deg}]$ | $\delta[\mathrm{deg}]$ | CR | Description |  |
| 1 | 19.3245 | $-9.2235 \cdot 10^{-9}$ | 210.16 | -20.47 | 12.9 | Due to H1 alone |
| 2 | 27.8422 | $-8.2416 \cdot 10^{-11}$ | 123.54 | -70.26 | 41.7 | Instrumental artifact mainly in L1 |
| 3 | 27.8425 | $-7.1820 \cdot 10^{-11}$ | 76.67 | -74.73 | 63.2 | Instrumental artifact mainly in L1 |
| 4 | 59.6054 | $-7.8884 \cdot 10^{-11}$ | 98.17 | -70.46 | 51.2 | Two nearby instrumental artifacts in H1 and L1 |
| 5 | 59.6053 | $-8.2416 \cdot 10^{-11}$ | 263.16 | 62.68 | 39.9 | Two nearby instrumental artifacts in H1 and L1 |
| 6 | 217.4516 | $+1.8249 \cdot 10^{-10}$ | 77.15 | -31.98 | 7.8 | Due to H1 alone |
| 7 | 231.6987 | $-1.4128 \cdot 10^{-9}$ | 288.08 | 36.63 | 9.0 | Consistent among H1 and L1. |
| 8 | 269.8699 | $-5.7679 \cdot 10^{-9}$ | 242.98 | 33.60 | 7.9 | Possibly transient disturbance in H1 |
| 9 | 281.5976 | $-2.5184 \cdot 10^{-9}$ | 166.49 | 44.47 | 7.8 | Consistent but not highly significant in single IFOs |
| 10 | 289.8485 | $-6.9783 \cdot 10^{-9}$ | 276.08 | 32.80 | 9.8 | Instrumental artifact in L1 |
| 11 | 294.5292 | $-1.1774 \cdot 10^{-10}$ | 316.32 | 30.28 | 7.9 | Possibly transient disturbance in H1 |
| 12 | 304.8360 | $-5.1687 \cdot 10^{-10}$ | 74.14 | -41.39 | 7.6 | Consistent among H1 and L1. |
| 13 | 393.3830 | $-7.2997 \cdot 10^{-10}$ | 37.59 | -24.43 | 7.7 | Not consistent among single IFOs |
| 14 | 456.9495 | $-3.0612 \cdot 10^{-10}$ | 248.33 | 44.97 | 8.0 | Consistent among H1 and L1. |

TABLE XI. Final outliers selected by the FrequencyHough pipeline. Each of them is identified by the frequency, the spin-down, the position in equatorial coordinates and the critical ratio computed on the corrected peakmap projection. Reference time is MJD $=57328.59684$ (GPS 1130509183.976).

| Idx | $\begin{gathered} \text { Frequency } \\ {[\mathrm{Hz}]} \\ \hline \end{gathered}$ | $\begin{gathered} \text { Spin-down } \\ {[\mathrm{nHz} / \mathrm{s}]} \\ \hline \end{gathered}$ | $\begin{gathered} \alpha \\ {[\mathrm{rad}]} \end{gathered}$ | $\begin{gathered} \delta \\ {[\mathrm{rad}]} \end{gathered}$ | $s_{\text {mean }}$ | \#cluster | \#L1 | \# H 1 | $s_{\text {L } 1}^{*}$ | $s_{\text {H1 }}^{*}$ | $s_{\text {max }}$ | $s_{\text {multi }}^{*}$ | $s_{\text {theo }}$ | Description |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6 | 52.8084 | -0.0175 | $-1.1478$ | $-1.4512$ | 24.22 | 975 | 554 | 20 | 20.36 | 40.54 | 27.02 | 45.61 | 45.20 | 1 |
| 9 | 53.8974 | 0.3693 | 0.4803 | 1.5115 | 6.31 | 14 | 6 | 3 | 5.66 | 10.47 | 6.50 | 21.20 | 11.90 | 2 |
| 14 | 57.0055 | -1.0014 | $-2.2336$ | -0.1685 | 9.84 | 14 | 7 | 2 | 15.84 | 9.17 | 11.43 | 14.28 | 15.37 | 3 |
| 24 | 62.4983 | 0.2480 | -1.0927 | 1.3699 | 14.64 | 1089 | 45 | 326 | 9.13 | 98.01 | 16.67 | 95.25 | 93.06 | 3 |
| 44 | 75.5055 | -0.9098 | -2.5598 | $-1.1455$ | 10.05 | 7 | 2 | 5 | 6.44 | 71.67 | 11.67 | 57.12 | 57.60 | 3 |
| 46 | 76.4988 | 0.2207 | $-1.1572$ | 1.2721 | 11.03 | 1090 | 34 | 282 | 7.59 | 76.60 | 11.49 | 68.14 | 67.41 | 3 |
| 47 | 77.4963 | 0.5741 | -0.1180 | 1.3766 | 9.54 | 959 | 70 | 121 | 6.28 | 76.87 | 10.61 | 70.23 | 66.58 | 3 |
| 49 | 78.4962 | 0.5587 | -0.2021 | 1.4096 | 9.65 | 308 | 13 | 129 | 6.38 | 75.89 | 10.29 | 69.25 | 64.34 | 3 |
| 52 | 79.9990 | 0.1808 | $-1.2674$ | 1.2599 | 10.05 | 615 | 59 | 175 | 6.59 | 107.63 | 10.90 | 97.21 | 91.77 | 3, 4 |
| 53 | 80.4994 | 0.0658 | $-1.5722$ | 1.2107 | 11.92 | 1254 | 97 | 138 | 7.41 | 68.79 | 13.27 | 60.94 | 60.89 | 3 |
| 60 | 84.4961 | 0.5454 | $-0.4443$ | 1.4369 | 8.95 | 1002 | 55 | 141 | 5.88 | 59.19 | 10.69 | 56.18 | 54.21 | 3 |
| 62 | 85.0013 | $-0.2165$ | 1.8264 | $-1.2866$ | 12.08 | 811 | 132 | 83 | 11.21 | 15.38 | 12.96 | 18.13 | 18.96 | 3 |
| 63 | 85.5012 | -0.1977 | 1.7877 | $-1.2674$ | 33.87 | 870 | 198 | 64 | 27.44 | 58.03 | 36.95 | 63.92 | 63.78 | 3 |
| 66 | 86.4989 | 0.1618 | $-1.4494$ | 1.2580 | 9.08 | 1357 | 147 | 125 | 6.38 | 57.24 | 10.49 | 54.70 | 53.67 | 3 |
| 76 | 98.4983 | 0.2876 | $-1.2383$ | 1.2866 | 10.16 | 1219 | 161 | 158 | 7.10 | 28.50 | 11.30 | 27.51 | 26.12 | 3 |
| 79 | 100.5032 | -0.5624 | 2.5925 | $-1.3402$ | 8.37 | 288 | 39 | 114 | 6.02 | 28 | 8.85 | 24.96 | 24.96 | 3 |
| 88 | 108.8573 | 0.0041 | $-3.1371$ | $-0.5718$ | 13.61 | 999 | 296 | 99 | 18.79 | 14.73 | 15.85 | 22.93 | 23.55 | 1 |
| 92 | 112.5026 | -0.4739 | $-1.8331$ | 0.9775 | 6.52 | 68 | 2 | 55 | 5.98 | 11.70 | 6.78 | 11.72 | 12.84 | 3 |
| 104 | 127.4964 | 0.5926 | $-0.9377$ | 1.3368 | 6.36 | 877 | 204 | 58 | 7.04 | 7.64 | 6.94 | 9.08 | 10.39 | 3 |
| 105 | 127.9988 | 0.2101 | $-1.3924$ | 1.2317 | 70.70 | 1165 | 161 | 70 | 61.13 | 108 | 78.07 | 123.85 | 121.24 | 3, 4 |
| 107 | 128.4984 | 0.3602 | $-1.1366$ | 1.2478 | 6.94 | 971 | 223 | 82 | 8.40 | 7.35 | 7.60 | 9.50 | 11.07 | 3 |
| 112 | 146.1994 | -6.6167 | 0.0500 | $-1.1133$ | 16.08 | 1676 | 796 | 22 | 15.96 | 22.10 | 18.11 | 27.17 | 26.87 | 1 |
| 136 | 191.0716 | -8.7553 | -0.2091 | $-0.5534$ | 22.83 | 988 | 262 | 107 | 30.61 | 22.80 | 25.66 | 37.00 | 37.76 | 1 |
| 153 | 255.9995 | 0.0789 | $-1.5493$ | 1.1792 | 30.62 | 1082 | 203 | 43 | 20.10 | 105.72 | 33.03 | 96.46 | 86.90 | 3, 4 |
| 160 | 265.5736 | 0.3441 | 1.1995 | $-0.9102$ | 21.16 | 750 | 286 | 18 | 24.76 | 25.97 | 25.19 | 35.18 | 35.85 | 1 |
| 193 | 452.8999 | $-2.7816$ | 2.5350 | $-1.3173$ | 10.01 | 222 | 4 | 109 | 6.68 | 88.07 | 10.04 | 61.91 | 28.21 | 5 |

TABLE XII. SkyHough outliers after population and multi-interferometer consistency vetoes. The table provides the frequency, spin-down and sky location of the cluster centers found by the SkyHough search. \#cluster is the size of the cluster in terms of number of coincident pairs, $s_{\text {max }}$ and $s_{\text {mean }}$ are the maximum and mean value of the cluster significance, $\#_{L 1}$ and $\#_{H 1}$ are the number of different candidates producing coincidence pairs from the different data sets, $s_{L 1}^{*}$ and $s_{H 1}^{*}$ are the maximum significance values obtained by analysing the data from H1 and L1 separately, $s_{m u l t i}^{*}$ is maximum combined significance when the data from both detectors are analyzed jointly and $s_{\text {theo }}$ is the expected theoretical combined significance value. Frequencies are converted to epoch GPS 1125972653. The outliers description codes mean the following: 1- hardware injection, 2- associated to unknown comb in H1 starting at 30.9430 Hz with 0.99816 Hz spacing, 3- miscellaneous combs with known or unknown sources at multiples of 0.5 Hz many of them due to blinking LEDs in timing system, 4 - associated with the 8 Hz comb in H 1 due to the OMC length dither, and 5 -spectral disturbance in H1.

| Idx | $\begin{gathered} \text { Frequency } \\ \mathrm{Hz} \\ \hline \end{gathered}$ | $\begin{gathered} \text { Spindown } \\ \mathrm{nHz} / \mathrm{s} \\ \hline \end{gathered}$ | $\begin{gathered} \text { RA }_{\mathrm{J} 2000} \\ \text { degrees } \\ \hline \end{gathered}$ | $\begin{gathered} \hline \text { DEC }_{\text {J2000 }} \\ \text { degrees } \\ \hline \end{gathered}$ | Description |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 12.49993 | 0.025 | 86.603 | -58.499 | 0.25 Hz comb |
| 2 | 12.50002 | -0.002 | 90.000 | 66.561 | 0.25 Hz comb |
| 3 | 31.76207 | -0.151 | 127.576 | 29.821 | PowerFlux idx 66 |
| 4 | 36.60793 | -0.416 | 161.240 | $-52.346$ | Present only in L1 |
| 5 | 36.60841 | -0.075 | 100.874 | 43.930 | Present only in L1 |
| 6 | 13.49980 | 0.055 | 93.007 | 58.722 | 0.25 Hz comb |
| 7 | 31.76213 | -0.029 | 121.201 | -22.659 | PowerFlux idx 66 |
| 8 | 85.82924 | -0.782 | 122.451 | 42.487 | Present only in H1 |
| 9 | 85.82951 | 0.014 | 91.251 | -60.424 | Present only in H1 |
| 10 | 83.44610 | 0.356 | 57.433 | 74.096 | Instrumental artifact |
| 11 | 83.44718 | -0.188 | 100.706 | $-71.727$ | Instrumental artifact |
| 12 | 26.30940 | 0.120 | 65.866 | 28.651 | PowerFlux idx 104 |
| 13 | 31.37813 | 0.076 | 86.489 | 60.660 | Hardware injection ip11 |
| 14 | 31.51095 | $-0.260$ | 125.878 | -30.969 | Hardware injection ip11 |
| 15 | 13.49954 | 0.028 | 103.846 | -33.555 | 0.25 Hz comb |
| 16 | 34.82444 | -0.178 | 125.214 | $-37.390$ | Present only in H1 |
| 17 | 34.82526 | 0.365 | 43.489 | 59.488 | Present only in H1 |
| 18 | 26.34245 | 0.188 | 101.305 | -41.914 | PowerFlux idx 104 |
| 19 | 52.80802 | 0.272 | 75.131 | 46.185 | Hardware injection ip5 |
| 20 | 52.80847 | -0.217 | 86.346 | -63.610 | Hardware injection ip5 |
| 21 | 19.90049 | -0.049 | 120.105 | -66.933 | Transient disturbance |
| 22 | 108.85713 | 0.016 | 172.077 | -30.650 | Hardware injection ip3 |
| 23 | 108.85751 | -0.190 | 156.197 | 11.273 | Hardware injection ip3 |
| 24 | 191.02943 | -8.248 | 19.785 | 8.689 | Hardware injection ip8 |
| 25 | 191.02921 | -8.461 | 10.399 | -26.263 | Hardware injection ip8 |
| 26 | 39.76317 | $-0.250$ | 116.156 | 35.030 | PowerFlux idx 77 |
| 27 | 39.76228 | -0.111 | 120.585 | -49.208 | PowerFlux idx 77 |
| 28 | 210.38111 | -0.719 | 111.146 | -73.636 | Present only in H1 |
| 29 | 146.16957 | $-7.664$ | 74.426 | 19.212 | Hardware injection ip6 |
| 30 | 146.16861 | -6.847 | 9.592 | -64.231 | Hardware injection ip6 |
| 31 | 46.94798 | 0.037 | 120.395 | 66.304 | PowerFlux idx 48 |
| 32 | 46.94859 | 0.059 | 107.507 | -49.753 | PowerFlux idx 48 |
| 33 | 93.89883 | 0.344 | 66.466 | 72.993 | Present only in H1 |
| 34 | 93.89971 | -0.084 | 94.143 | -67.379 | Present only in H1 |
| 35 | 33.33199 | 0.186 | 82.235 | 49.267 | Present at the beginning in H1 and in the middle in L1 |
| 36 | 33.33191 | 0.147 | 101.592 | -24.740 | Present at the beginning in H1 and in the middle in L1 |
| 37 | 28.94735 | -0.023 | 80.524 | -62.043 | Present only in H1 |
| 38 | 28.94644 | 0.217 | 56.600 | 61.593 | Present only in H1 |
| 39 | 140.25111 | -0.261 | 118.249 | 65.668 | 0.25 Hz comb |
| 40 | 273.76680 | 0.022 | 279.363 | $-0.225$ | Present only in the first half of O1 |
| 41 | 66.75634 | 0.060 | 67.002 | 65.771 | Present only in H1 |
| 42 | 286.11848 | 0.220 | 282.207 | 7.749 | Present only in the first half of O1 |
| 43 | 27.94841 | 0.150 | 79.648 | -46.995 | Present only in H1 |
| 44 | 65.87802 | -0.007 | 95.671 | 68.015 | Present only in H1 |
| 45 | 65.87734 | 0.237 | 82.021 | -39.834 | Present only in H1 |
| 46 | 265.57578 | $-0.077$ | 71.932 | -57.608 | Hardware injection ip0 |
| 47 | 364.34662 | 0.322 | 281.187 | 22.135 | Present only in the first half of O1 |
| 48 | 43.74991 | -0.110 | 87.628 | -41.298 | 0.25 Hz comb |
| 49 | 331.65142 | 0.296 | 301.174 | -56.957 | Present only in the first half of O1 |

TABLE XIII. Time-Domain $\mathcal{F}$-statistic pipeline outliers in the range of frequencies between 10 and 475 Hz . The columns provide the nominal frequencies and frequency derivatives, right ascensions and declinations found for the outliers, along with comments indicating the likely sources of the outliers.


FIG. 22. Peakmap projections for outlier 7 of the FrequencyHough search. The dotted blue line is for Hanford detector analysis, the green dashed line is for Livingston detector analysis and the continuous black line is for the joint search.


FIG. 23. Joint Hough map for outlier 7 of the FrequencyHough search.
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